## Tunable Gauge Potential for Neutral and Spinless Particles in Driven Optical Lattices

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We present a universal method to create a tunable, artificial vector gauge potential for neutral particles trapped in an optical lattice. The necessary Peierls phase of the hopping parameters between neighboring lattice sites is generated by applying a suitable periodic inertial force such that the method does not rely on any internal structure of the particles. We experimentally demonstrate the realization of such artificial potentials, which generate ground-state superfluids at arbitrary nonzero quasimomentum. We furthermore investigate possible implementations of this scheme to create tunable magnetic fluxes, going towards model systems for strong-field physics.

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First introduced in electromagnetism, gauge fields play a central role in the description of interactions in physics, from particle physics to condensed matter. Currently, there is a large interest to introduce gauge fields into model systems in order to study fundamental aspects of physics [1]. In particular, the emulation of synthetic electric and magnetic fields for ultracold atomic systems is crucial in order to extend their proven quantum simulation abilities further, e.g., to quantum Hall physics or topological insulators. Since the studied atomic systems are neutral, the forces acting on a charged particle in a magnetic or electric field are absent here. Thus, the emulation of analog effects on the center-of-mass motion of each atom requires "artificial" gauge potentials. In this context, the analogy between inertial and Lorentz forces triggered the simulation of homogeneous artificial magnetic fields using rapidly rotating trapped ultracold gases [2]. Recently, several proposals ([3,4] and references therein) and experimental realizations focused on the simulation of a gauge vector potential A either in a bulk system [5,6] or in optical lattices [7–9]. The realized schemes exploit the Berry phase which arises when the atomic ground state is split in several space-dependent sublevels, as in the presence of an electromagnetic field. Hence, they rely on the coupling between internal and external degrees of freedom induced by laser fields.

Here we demonstrate the generation of artificial gauge potentials for neutral atoms in an optical lattice without any requirements on the specific internal structure. As the realized scheme only relies on the trapability of the particle, it can be very widely applied to many atomic systems, and also to molecules and other complex particles. It is particularly interesting for fermionic systems, where, in a many-body state governed by the Pauli principle, the use of internal degrees of freedom often leads to conflicts with the creation of gauge potentials. As an important additional benefit, the internal degrees of freedom of the particles can be addressed independently, e.g., by real magnetic fields or microwave excitations.

In general, the presence of a gauge vector potential modifies the kinetic part of the Hamiltonian describing the system. In a lattice, an artificial field can then be simulated by engineering a complex tunneling parameter  $J = |J|e^{i\theta}$ , where  $\theta$  is the Peierls phase.

The central approach here is to control this phase via a suitable forcing of the lattice potential, acting at the singleparticle level. We describe the general scheme for the creation of an artificial gauge potential and experimentally demonstrate the realization of a tunable vector gauge potential in 1D. We analyze the dynamical processes leading to the relaxation toward a superfluid ground state at any desired, finite quasimomentum. In a 2D lattice the described forcing can be used to create artificial magnetic fluxes smoothly tunable between  $-\pi$  and  $\pi$ . For a maximal flux of  $\pi$  through an elementary plaquette, strong-field physics as, e.g., the Hofstadter spectrum, could be emulated. To reach this limit with condensed matter systems, magnetic fields of several thousand Tesla would be required, which is up to now beyond experimental possibilities.

For the general scheme, we consider a system of ultracold atoms in a deep optical lattice described by the Hubbard-type tight-binding Hamiltonian:

$$\hat{H}(t) = -\sum_{\langle ij\rangle} J_{ij} \hat{a}_i^{\dagger} \hat{a}_j + \sum_i v_i(t) \hat{n}_i + \hat{H}_{\text{on-site.}}$$
(1)

Here  $\hat{a}_i^{\dagger}$ ,  $\hat{a}_i$ , and  $\hat{n}_i$  denote the creation, annihilation, and number operator for a particle (boson or fermion) of mass

*m* localized at site *i* at  $\mathbf{r}_i$ ;  $J_{ij} > 0$  quantifies the tunneling between neighboring sites, and  $\hat{H}_{on-site}$  comprises timeindependent on-site terms describing, e.g., interactions or a trapping potential. The system is driven by fast, offresonant time-periodic potential modulations  $v_i(t) =$  $v_i(t + T)$  of zero time average  $\langle v_i \rangle_T \equiv \frac{1}{T} \int_0^T dt v_i(t)$  with period *T*. The case of a homogeneous inertial force  $\mathbf{F} =$  $-m\ddot{\mathbf{x}}$ , which is created by shaking the lattice along the periodic orbit  $\mathbf{x}(t)$  in space [see Fig. 1(a)], is described by  $v_i = -\mathbf{r}_i \cdot \mathbf{F}$ . Under the conditions described in Ref. [10], one can show that the driven system is to good approximation described by the effective time-independent Hamiltonian:

$$\hat{H}_{\text{eff}} = -\sum_{ij} |J_{ij}^{\text{eff}}| e^{i\theta_{ij}} \hat{a}_i^{\dagger} \hat{a}_j + \hat{H}_{\text{on-site}}.$$
 (2)

The important terms here are the complex tunneling parameters  $|J_{ij}^{\text{eff}}|e^{i\theta_{ij}} = J_{ij} \langle e^{i(\chi_j - \chi_i)/\hbar} \rangle_T$  (see Fig. 1), where  $\chi_i(t) = -\int_{t_0}^{t} dt' v_i(t') + \langle \int_{t_0}^{t} dt' v_i(t') \rangle_T$ . For sinusoidal forcing, such a dynamic modification of tunneling is restricted to  $\theta_{ij} = 0$  or  $\pi$  [11–14]. It has recently been observed in several experiments [15–18]. We will now show that by suitable driving, the Peierls phases  $\theta_{ij}$  can in fact be smoothly tuned to any value  $\theta \in [0, 2\pi[$ . This allows one to engineer vector potentials that can give rise to both artificial electric and magnetic fields. Similar ideas have recently been presented for a Bose-Fermi mixture in a triangular lattice [19].

The Peierls phase  $\theta_{ij}$  can be varied smoothly, even though  $\langle \chi_i \rangle_T = 0$ . Indeed,  $\langle e^{i(\chi_j - \chi_i)} \rangle_T$  can be complex provided the forcing breaks two symmetries that are also known to prevent ratchet-type rectification in classical [20] and quantum [21] lattice systems, namely, (a) reflection symmetry for a suitable time  $\tau$ , i.e.,  $v_i(t - \tau) = v_i(-t - \tau)$ 



FIG. 1 (color). Periodic driving of the 1D lattice. (a) Timeperiodic movement of the lattice in real space. (b) Resulting periodic inertial force of zero mean.  $T_1/T_2$  is the asymmetry parameter. (c) Realized complex tunneling elements on a 1D lattice, with spacing *d*. (d) Effective single-particle dispersion relation. A complex phase induces a shift of  $E_{\rm eff}(k)$  toward  $k_{\rm min} = \theta/d$  (solid line).

and (b) shift (anti)symmetry, i.e.,  $v_i(t - T/2) = -v_i(t)$ . This requires forcing with more than one frequency. The forcing function used in our experiment [see Fig. 1(b)] induces a monotonically increasing Peierls phase  $\theta_{ij} = \arg(\langle e^{im\dot{x}\cdot(r_j-r_i)}\rangle_T)$  with the amplitude of the force.

The Peierls substitution directly links this phase to a gauge vector potential A via  $\theta_{ij} = \int_{r_j}^{r_i} d\mathbf{r} \cdot A/\hbar$  (integrated along a straight path), which allows us to create artificial electric or magnetic fields. The modification of the Peierls phase in time results in an artificial electric force  $F_E = -\dot{A}$ . The term "artificial" stresses here that the generated field is not an usual electric field (as known from Maxwell's theory). Our artificial electric field, however, affects the particles quasimomentum, in the same manner. It will be shown at the end of this Letter that our scheme allows the emulation of a vector potential that gives rise to a finite artificial magnetic flux through the elementary plaquettes of 2D lattices.

To demonstrate the power of this scheme, we have emulated a vector potential for a rubidium Bose-Einstein condensate (BEC) in a one-dimensional lattice. The trapped particles are accelerated via frequency modulation of one of the lattice beams, a technique which is experimentally straightforward. The resulting inertial force is comprised of a train of sinusoidal pulses separated by periods of rest of periodicity  $T = T_1 + T_2 = 1$  ms as depicted in Fig. 1(b). The zero mean value of this force prevents the transfer of a net acceleration to the lattice. This leads to a renormalized tunneling matrix element of the form,

$$\frac{J^{\text{eff}}(K)}{J^{\text{bare}}} = \frac{T_2}{T} e^{iK(T_1/T)} + \frac{T_1}{T} J_0(K) e^{-[iK(T_2/T)]}$$
(3)

where  $T_1/T_2$  is the asymmetry parameter; K is the forcing amplitude [22], and  $J_0(K)$  the zero-order Bessel function. From Eq. (3), the induced Peierls phase  $\theta$  in the effective tunneling element can be calculated. For  $T_2/T \rightarrow 0$ , one recovers the harmonic driving introduced in [14] which only allows us to control the magnitude and sign of  $J^{\text{eff}}$ . In the opposite limit of small  $T_1/T$ , the tunneling amplitude  $|J^{\rm eff}|$  is only marginally affected whereas the phase  $\theta$ depends linearly on the forcing amplitude K. In order to avoid unwanted excitations of the system induced by strong forcing, we have chosen an intermediate value  $T_1/T_2 = 2.1$  for the experiment realized here. Note, however, that for such an asymmetry parameter, the Peierls phase depends nonlinearly on K [see Fig. 2(b)]. The introduced gauge potential  $A = \hbar \theta / d$  manifests itself via a shift of the dispersion relation by  $\theta/d$  as depicted in Fig. 1(d). This follows directly from the effective Hamiltonian (2), whose eigenstates are Bloch waves with the dispersion relation  $E(k) = -2|J^{\text{eff}}|\cos(kd - \theta)$ . The gauge potential therefore allows for the generation of superfluid ground states (with group velocity  $v_g = dE/dk = 0$ ) at finite and tunable quasimomentum



FIG. 2 (color). Creation of complex tunneling matrix elements. (a) Absolute value of the tunneling parameter obtained from Eq. (3) for our experimental parameters  $(T_1 + T_2 = 1 \text{ ms} \text{ and } T_1/T_2 = 2.1)$ . (b) The measured Peierls phases in a 1D driven optical lattice for different values of the forcing amplitude *K* are depicted as circles. The dashed red curve corresponds to the theoretically expected values [Eq. (3)]. (c) Quasimomentum distribution of the BEC after 27 ms time of flight for different values of *K*. The Peierls phase as a function of *K* is deduced from the observed shifts of the interference patterns.

 $k = A/\hbar$ . As will be detailed later on, we experimentally observe the relaxation of the condensate quasimomentum toward the minimum of the effective dispersion relation. Therefore, the imprinted Peierls phase can be directly read out from the quasimomentum distribution revealed in the time of flight after a sudden switch off of the lattice and the external potential.

As a central result, Fig. 2(b) shows the experimental data together with the theoretical predictions from Eq. (3). After increasing the forcing amplitude slowly (within up to 120 ms) to the desired value, the corresponding quasimomentum distribution was recorded. From the obtained time-of-flight images, examples of which are shown in Fig. 2(c), we extract the Peierls phases  $\theta$  [22]. We observe an excellent agreement between experiment and theory, thus proving the controlled generation of an arbitrary vector gauge potential encoded into the Peierls phase  $\theta \in [0, 2\pi[$ . In addition, the experimental images demonstrate the large degree of coherence maintained in the atomic sample throughout the shaking process. As an additional feature, Fig. 2(a) shows that the Peierls phase allows us

now to invert the sign of the effective tunneling element without crossing  $|J^{\text{eff}}| = 0$  via the rotation in the complex plane.

In the following, we will discuss the details of the relaxation of the system toward nonzero quasimomenta superfluid states, allowing for the described direct measurement of the Peierls phase. Note that for an homogeneous and noninteracting system, the initial Bloch wave at  $k_i = 0$  remains an eigenstate of the effective Hamiltonian. Thus, no transfer to states with  $k \neq 0$  is expected after the shaking is turned on. However, since we are working with interacting bosons and an external harmonic confinement, more effects come into play.

When the gauge potential is ramped up from 0 to  $A_f$ , the condensate acquires a nonzero group velocity, reflecting the presence of an artificial electric force  $F_E = -\dot{A}$ . This velocity induces a displacement of the condensate's centerof-mass position  $x_c$  in the harmonic potential of frequency f [22]. The resulting restoring force induces oscillations both in position and momentum space [see Fig. 3(a)]. In Fig. 3(b), we report a time-resolved measurement of the condensate quasimomentum after a quench to a final Peierls phase of  $-\pi/4$ . The oscillations around the final quasimomentum result from an excitation of the dipole mode: The measured frequency of  $3.6 \pm 0.4$  Hz perfectly matches the expected dressed condensate frequency  $\sqrt{m/m^*}f$  for particles having an effective mass  $m^*$  in the lattice of  $10 \pm 1E_{\rm rec}$  depth with a tunneling amplitude of  $0.3J_{\text{bare}}$  ( $f_{\text{theo}} = 3.5 \pm 0.5$  Hz). The coupling to nonzero quasimomenta results thus from the underlying harmonic trapping potential.

In addition, this center-of-mass dynamics is subjected to several damping mechanisms induced by the trap anharmonicity or the lattice discreteness, which leads to a coupling to other collective modes and therefore to the relaxation of the BEC toward the new equilibrium state. Therefore, the duration of the ramp from 0 to  $A_f$  has to be compared with the time scale of those relaxation mechanisms. In Fig. 3 we compare time-resolved measurements of the quasimomentum distribution for a slow ramp [Fig. 3(d)] of A to a final Peierls phase  $\theta = 3\pi/2$ , with a sudden quench [Fig. 3(f)]. As the gauge field is slowly increased, the BEC follows the shift of the dispersion relation minimum, as depicted in Fig. 3(c). For the quench, on the contrary, for which the shift of the dispersion relation occurs within 1 ms, the system cannot follow and thus relaxes into the nearest minimum of the effective band structure [see Fig. 3(e)]. For the chosen value, this minimum lies on the left with respect to the original k = 0peaks and we thus find the BEC at  $k = -\pi/2d$ . This demonstrates clearly that in the presence of these relaxation mechanisms, the forcing does not induce a net particle current in the lattice, unlike for ratchets, but allows the engineering of ground-state superfluids at arbitrary nonzero quasimomenta.



FIG. 3 (color). Time-resolved measurements. (a), (b) A quench to a Peierls phase of  $-\pi/4$  within 1 ms induces an excitation of the dipole mode, leading to oscillations of the quasimomentum as depicted in (a) and observed in the timeresolved measurement of the quasimomentum up to 0.5 s. (b). The plain curve is a fit to a sinusoid from which one obtains  $f_{\rm exp} = 3.6 \pm 0.4$  Hz, in perfect agreement with the expected dipole frequency of the dressed condensate. The final value of the Peierls phase is depicted as a dashed line. (c)–(f) Shift of the quasimomentum toward a final Peierls phase of  $3\pi/2$  for a slow increase of the forcing amplitude over 160 ms (c), (d) or a sudden quench within 1 ms (e), (f). The left graphs depict the center-of-mass dynamics in k space in both cases. On the right, a series of time-of-flight images are reported as a function of time. The time steps are 10 ms and 1 ms, respectively.

Our scheme to generate complex tunneling offers fascinating possibilities to emulate gauge fields in higher dimensions. In the following, a few examples based on lattice shaking and modulated superlattices will be described. An artificial magnetic field is characterized by a finite magnetic flux through an elementary plaquette P of the lattice, given by the sum  $\Phi_P = \theta_{ij} + \theta_{jk} + \cdots + \theta_{li} \mod 2\pi \in$  $(-\pi, \pi]$  taken around P. Homogeneous forcing, implemented by lattice shaking, cannot give rise to a magnetic flux through plaquettes having pairwise parallel edges like square or hexagonal. It can, however, lead to a nonzero flux  $\phi_{\Delta}$  through a triangular plaquette;  $\phi_{\Delta} = \theta(|F_0|d) - \theta(|F_0|d)$  $2\theta(|F_0|d/2)$  for  $F_0$  the amplitude of the force oriented parallel to one edge. As depicted in Fig. 4(a), continuously tunable staggered fluxes are realized ( $\phi_{\nabla} = -\phi_{\Delta}$  for the inverted plaquette). Our method enables one to continuously control the degree of frustration from zero ( $\phi_{\Delta} = 0$ ) to maximum ( $\phi_{\Delta} = \pi$ ) in lattice geometries like triangular



FIG. 4 (color). Creation of magnetic fluxes in triangular lattices. (a) Staggered magnetic fluxes obtained in a 2D triangular lattice. (b) Dispersion relation for different values of the magnetic flux  $|\Phi|$  through a plaquette.

or kagome [23,24]. This control can be used to adiabatically prepare and study exotic quantum phases that are expected to appear in the strongly frustrated limit. Increasing the flux in a triangular lattice, frustration is reflected in the fact that the dispersion relation develops two minima that eventually, for  $\pi$  flux, become degenerate [see Fig. 4(b)]. In a triangular lattice with  $\pi$  flux, spontaneous symmetry breaking has recently been observed in an experimental simulation of classical magnetism [18]. With the presented scheme, one is now able to study the influence of a small symmetry-breaking perturbation and to observe the many-body dynamics initiated by preparing a system in the upper minimum.

Tunable magnetic fluxes through, e.g., square or hexagonal plaquettes can also be obtained via inhomogeneous forcing. A simple way of doing this is to create an oscillating superlattice as will be described elsewhere.

Beyond the engineering of the hopping element, another essential feature of our scheme is the possibility to address the atomic internal degrees of freedom independently. Here, a spin-dependent hexagonal lattice [25] constitutes a promising system. In such a geometry, the interplay of next-nearest neighbor coupling, complex tunneling matrix elements, and spin are particularly interesting in connection with Haldane's model, for instance [26,27]. The very general method presented in this Letter should allow for large sets of new gauge fields schemes for various particle classes in optical lattices.

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