Plastic Quantum Crystals

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Compared to classical solids, the quantum solid helium-4 can undergo a giant plastic deformation that is also reversible.

Subject Areas: Superfluidity, Quantum Physics

A Viewpoint on:
Giant Plasticity of a Quantum Crystal
Ariel Haziot, Xavier Rojas, Andrew D. Fefferman, John R. Beamish, and Sébastien Balibar

If you bend a piece of metal into a new shape, it will not spontaneously revert to the condition in which it started. The reason is that bending causes the metal to undergo a plastic deformation: an irreversible change of shape that occurs when an applied load exceeds a certain threshold. In Physical Review Letters, Ariel Haziot at the École Normale Supérieure in Paris, France, and colleagues report that the plastic properties of a “quantum solid,” helium-4, can be strikingly different: in helium-4, within a certain temperature range, large plastic deformations can still be reversible [1]. The findings highlight the unusual mechanical properties of quantum solids, and may serve as a model system for understanding the fundamental mechanisms contributing to plasticity.

Plasticity is the propensity of solids to “flow.” It is usually the result of the motion of dislocations, which are crystallographic defects in the form of lines of misfit between atomic planes. In a crystal with dislocations, a moderate shear can generate plastic flow by causing the dislocations to move. The effect is reminiscent of how the movement of a hump in a heavy carpet can be used to slide a carpet on a floor without having to move the whole carpet. Indeed, an ideal, defect-free classical crystal can’t flow, but only respond elastically to shear. This is why mechanical pieces that have to withstand tremendous stress, such as turbine blades, are now made of monocrystalline materials [2]—a possibility thanks to advances in crystal growth techniques, which can now avoid the presence of any dislocation. In the past, when single crystals could not be made free of dislocations, stiffness was restored through impurities, which act as pinning centers that lock dislocations in place, or by multiplying the number of dislocations so that they would pin each other.

Large plasticity thus relies on the presence of many dislocations that can easily move through the crystal. Not all crystal types, however, can accommodate a large number of dislocations. In a solid held together by covalent atomic bonds, dislocations can only move by breaking localized chemical bonds. Such materials are brittle, breaking easily. In contrast, the bonding in metals is not due to localized bonds, but to delocalized conduction electrons. Dislocations do not easily break metals and the ease of their motion explains why many metals are so malleable.

Delocalized bonds are also characteristic of other, more exotic types of solids: quantum crystals. These crystals are made up of atoms, like helium, or molecules, like hydrogen, that are so light that nuclear quantum effects become important, and new, nonclassical theories are needed to describe them. In quantum crystals, delocalization of bonds is the consequence of the lightness of atoms or molecules, which gives them, according to quantum mechanics, a large zero-point motion, i.e., a large excursion around their average position in the crystal. Since quantum crystals have highly mobile dislocations, their plasticity is often found to exceed that of normal materials.

Haziot et al. carried out a detailed study of the plasticity properties of solid helium-4, exploiting a novel experimental setup in which they can monitor the crystals, control their orientation, growth, and quality, and at the same time, measure their elastic moduli along different directions. Their results show that, in a certain temperature range, the crystal exhibits a giant plasticity that is reversible (the solid goes back to its original shape when the applied stress is released) and anisotropic (the solid flows with little resistance when shear is applied in a specific direction) [4].

Strictly speaking, what Haziot et al. observe is more of an elastic deformation than a conventional plastic one. In classical crystals, plasticity is, by definition, irreversible. However, Haziot et al. show that one of the elastic moduli of the crystal is dramatically reduced (by a factor of 3) compared to what is expected for a perfect crystal, and they carry out a number of tests to understand the origin...
of such behavior. The fact that, of the six different elastic
moduli describing solid helium-4, only the shear modulus
\( C_{44} \) is modified, and that the reduction in this modulus
depends on the crystal growth and the number of helium-3
impurities, indicates that the effect is due to the motion
doing dislocations, like for plasticity.

The mechanisms underpinning such large plasticity can
be explained in the following way. Solid helium-4 has a
hexagonal crystal structure and it is known that in such
structures dislocations slip easily in the so-called basal
plane, which is perpendicular to the long axis (c-axis) of
the crystal. What prevents unlimited shear-induced flow
along this plane are impurities, which pin the dislocations
at various points (as illustrated in Fig. 1), or interactions
between different dislocations. Under a shear stress, dis-
locations bend like strings between their pinning centers.
The amplitude of their displacement is proportional to
the applied stress, and gets larger when the distance be-
tween pinning centers is larger. This mechanism explains
the anisotropy and why the effect is larger in higher qual-
ity crystals, which have fewer pinning centers and thus
a larger average distance between them. Since no irre-
versible jumps from one pinning center to another are in-
volved, but only elastic extension of the dislocations, the
behavior is reversible. In helium-4, pinning centers could
partly consist of impurities of helium-3, the lighter iso-
tope of helium. Such impurities can diffuse in the crystal
and condense on dislocations cores, where they find more
room for their large zero-point motion, reducing their ki-
netic energy. Once condensed on a dislocation, they pin
it, blocking its motion and restoring the standard elastic
response. But above a certain threshold of applied stress,
the dislocation can release itself from helium-3 impuri-
ties, which diffuse too slowly to follow it. This unpinning
of dislocation lines is what leads to the large propensity
to flow observed by the authors.

Such mechanisms are not the sole prerogative of quan-
tum crystals. The modification of the elastic moduli due
to the reversible motion of dislocations has indeed been
seen in classical crystals [3], but it is so tiny that it only
becomes measurable when dislocations resonate with one
another, like strings, with the applied oscillating stress.
The effect only occurs in a narrow frequency range and
appears as a frequency-dependent damping mechanism
for sound [3]. In quantum helium-4 crystals, however,
the huge amplitude of the effect is due to the high qual-
ity of the crystals and to the absence of damping mech-
ani on for the solid’s giant plasticity. The figure sketches two con-
cutive basal planes (blue and red atoms) within the hexag-
onal crystal structure of helium-4. Dislocations (marked by
a dashed line) are pinned by helium-3 impurities (in cyan),
which have a larger zero-point motion than helium-4. Dis-
locations can easily slide on the basal plane, enabling large
plastic deformations of the crystal when shear stress is ap-
p. (APS/Alan Stonebraker)

FIG. 1: According to Haziot et al., the movement of dislo-
cations on the basal plane of helium-4 crystals is responsible
for the solid’s giant plasticity. The figure sketches two con-
nsecutive basal planes (blue and red atoms) within the hexag-
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for interpreting the puzzling experimental results of Kim
and Chan [4]. Kim and Chan observed that helium-4
solids are unexpectedly able to flow when rotated in a
container at low temperature, which led to the controver-
sial speculation that helium-4 could be a “supersolid,” a
solid that flows with zero viscosity. Several experi-
mentalists, including Chan himself, have now concluded that
this interpretation was probably not correct (see 8 Oc-
tober 2012 Focus). Instead, alternative theories, such as
the one proposed by Varoquaux [5] have attempted to
explain such observations without invoking supersol-
arity. Such theories could be corroborated by Haziot et
al.’s analysis. These findings are also a motivation for
reevaluating the yet-to-be-understood results concerning
the plasticity of other quantum crystals, such as the anom-
aalous plasticity of hydrogen crystals reported recently [6].
Finally, the paper of Haziot et al. illustrates a remarkable
example of how the study of quantum crystals unveils
mechanisms that are hard to observe in more classical
systems.

References
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Bernard Castaing is a professor at the École Normale Supérieure (ENS), Lyon. He received his Ph.D. in 1978 under Albert Libchaber at the ENS. He was professor at the Joseph Fourier University, visiting professor at the James Franck Institute in Chicago, and has directed the Institut de Physique de la Matière Condensée in Grenoble. He has carried out extensive research in condensed-matter physics and hydrodynamics, including the study, both experimental and theoretical, of Rayleigh–Bénard convection, electron-phonon interaction in metals, turbulence, and superfluid helium. Among various honors, he was a recipient of the IBM prize (1984) and was appointed Member of the French Academy of Science in 2003.