Single-Photon Transistor Mediated by Interstate Rydberg Interactions

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We report on the realization of an all-optical transistor by mapping gate and source photons into strongly interacting Rydberg excitations with different principal quantum numbers in an ultracold atomic ensemble. We obtain a record switch contrast of 40% for a coherent gate input with mean photon number one and demonstrate attenuation of source transmission by over ten photons with a single gate photon. We use our optical transistor to demonstrate the nondestructive detection of a single Rydberg atom with a fidelity of 0.72(4).

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In analogy to their electronic counterparts, all-optical switches and transistors are required as basic building blocks for both classical and quantum optical information processing [1, 2]. Reaching the fundamental limit of such devices, where a single gate photon modifies the transmission or phase accumulation of multiple source photons, requires strong effective interaction between individual photons. Engineering sufficiently strong optical nonlinearities to facilitate photon-photon interaction is one of the key goals of modern optics, and immense progress towards this goal has been made in a variety of systems in recent years. Most prominent so far are cavity QED experiments, which use high finesse resonators to enhance interaction between light and atoms [3–7] or artificial atoms [8–11]. In particular, an optical transistor with high contrast and high optical gain operated by a single photon stored in an atomic ensemble inside a cavity has recently been demonstrated [12]. Cavity-free approaches include single dye molecules [13] and atoms coupled to hollow-core [14, 15] and tapered nanofibers [16].

A novel free-space approach to realize single-photon nonlinearities is to map strong interaction between Rydberg atoms [17] onto slowly travelling photons [18, 19] using electromagnetically induced transparency (EIT) [20]. This has already been used to demonstrate highly efficient single-photon generation [21], attractive interaction between single photons [22], entanglement generation between light and atomic excitations [23], and most recently single-photon all-optical switching [24].

However, demonstration of amplification, that is, controlling many photons with a single one, has so far only been achieved in a cavity QED setup [12]. Gain $\gg 1$ is one of the key properties of the electric transistor that lies at the heart of its countless applications. Here, we demonstrate an all-optical transistor with optical gain $G > 10$. We employ two-color Rydberg EIT in a free-space ensemble to independently couple gate and source photons to different Rydberg states [25]. For a coherent gate pulse containing on average one photon, we observe a switch contrast of $C_{\text{coh}} = 0.39(4)$, defined as

$$C = 1 - \frac{\bar{N}_{\text{s, out}}^{\text{with gate}}}{\bar{N}_{\text{s, out}}^{\text{no gate}}},$$

where $\bar{N}_{\text{s, out}}^{\text{with gate}}$ and $\bar{N}_{\text{s, out}}^{\text{no gate}}$ denote the mean numbers of transmitted source photons with and without gate photons. From this we extrapolate that a single-photon Fock state gate pulse causes a switch contrast $C_{g} = 0.53(2)$. The measured switch contrast is robust against the number of incoming source photons, enabling us to attenuate the source transmission by 10 photons with a coherent gate photon input with mean photon number $\bar{N}_{g, \text{in}} = 0.75(3)$. Finally, we use our transistor to implement single-shot non-destructive detection of single Rydberg atoms in a dense ultracold ensemble [26, 27]. Similar experiments have recently been performed by Tiarks et al. [28].

The level scheme and geometry of our transistor are illustrated in Fig. 1(a) and 1(b). Photons in the weak gate field $\mathcal{E}_{g}$ are stored as Rydberg excitations in an atomic ensemble by coupling the ground state $|g\rangle$ to the Rydberg state $|r_{g}\rangle$ via the strong control field $\Omega_{g}$ with an intermediate state detuning $\delta_{g}$ in a two-photon Raman process. After this storage process, the source field $\mathcal{E}_{s}$ is sent through the medium at reduced velocity due to resonant EIT provided by the control field $\Omega_{s}$ coupling to the Rydberg state $|r_{s}\rangle$. In the absence of a gate excitation and at a low source photon rate, individual source photons travel through the transparent medium. The strong van-der-Waals interaction between the Rydberg states $|r_{g}\rangle$ and $|r_{s}\rangle$ lifts the EIT condition within the interstate blockade radius $r_{gs}$ around a gate excitation. In this blockaded volume, the atomic level structure reduces to an absorbing two-level system, i.e., transmission of source photons is attenuated by scattering from the intermediate state [25]. To observe this conditional switching, we record the number of transmitted source photons in a time interval $t_{\text{int}}$ after the gate excitation pulse, cf. Fig. 1(c).
For our choice of Rydberg states |r_i⟩ and |r_g⟩, the interstate interaction energy becomes larger than ΔE_{EIT} at distances r_{gg} ≈ r_{ss} ≈ r_{gs} ≈ 15 μm, the blockade radii of the state combinations involved in our scheme. As r_{gs} is significantly larger than the radial extent of the gate and source beams, the essential requirement for an efficient transistor is met.

We first investigate the transistor performance for a weak source input photon rate R_{s,in} = 0.69(1) μs⁻¹. In Fig. 2(a) we plot the switch contrast in the source beam transmission as a function of the mean incoming gate photon number N_{g,in}. Source photon detection spans an integration time of t_{int} = 30 μs to acquire significant statistical data, yet t_{int} is small compared to the temperature limited retention time of the gate excitation in the source beam volume. For an average gate photon number of $\bar{N}_{g,in} = 1.04(3)$, we observe a switch contrast $C_{coh} = 0.39(4)$. The switch contrast is mainly determined by the Poissonian statistics of our coherent gate photons. Given $\bar{N}_{g,in}$, the probability to have zero photons in such a gate pulse is p(0) = e^{-\bar{N}_{g,in}} which sets a fundamental upper bound to the switch contrast, in other words, a perfect switch with coherent gate photons has a switch contrast $C_{coh} = 1 - e^{-\bar{N}_{g,in}}$ [dashed line in Fig. 2(a)]. How close our switch approaches this fundamental limit depends on the gate photon storage efficiency and the source attenuation caused by a single gate excitation. To estimate the storage efficiency, we monitor the gate pulse transmission $\bar{N}_{g,out}$ and take into account the finite absorption $A_{ge} = 0.15$ of gate photons from the intermediate level |e⟩ (measured independently at $\Omega_g = 0$). The mean number of stored gate photons is given by

$$N_{g,st} = (1 - A_{ge}) \cdot \bar{N}_{g,in} - \bar{N}_{g,out}. \tag{2}$$

In Fig. 2(b) we plot the switch contrast versus $\bar{N}_{g,st}$. We note that this estimate is an upper limit, as there may be...

*FIG. 2 (color online). Switch contrast (red) as function of (a) mean number of incident gate photons and (b) mean number of stored photons according to Eq. (2). The dashed line indicates the fundamental limit set by the photon statistics of the coherent gate input. Black data points represent the calculated switch contrast expected for (a) one-, two- and three-photon Fock input states or (b) deterministic single and two stored gate excitations.*
mechanisms removing gate excitations before or during the
switch operation but not resulting in a gate photon count.
These processes cannot be significant, though, as our
corrected switch contrast measurement in Fig. 2(b) would
then become better than the fundamental limit for gate
excitations following Poissonian statistics.

To extract the mean switch contrast caused by a single
incoming gate photon Fock state, we take into account the
photon statistics of the gate pulses and the saturation of gate
photon storage due to Rydberg blockade. The calculated
gate-gate blockade radius \( r_{gg} \approx 15 \mu m \) suggests that it
becomes very unlikely to store more than 3 gate photons
simultaneously, which is in agreement with the observed
storage efficiency for large \( N_{g,in} \). Assuming that a single
incoming gate photon causes an attenuation of the source
beam by \( e^{-OD_{st}} \), we write the expected switch contrast as

\[
C(N_{g,in}) = 1 - \sum_{k=0}^{\infty} \frac{N_{g,in}^k e^{-N_{g,in}}}{k!} e^{-\text{min}(k,3) \cdot OD_{st}},
\]

where we account for the blockade by allowing all photon
number states \( k > 3 \) to contribute only three gate exci-
tations. This simple model is motivated by more sophisti-
cated work on statistics of hard rods \[29\] and fits our data
very well. Applying the model from Eq. (3) to our data
[solid line in Fig. 2(a)] we obtain \( OD_{st} = 0.75(5) \) caused
by a single incoming gate photon. We stress that this value
does not correct for any loss or imperfections of our switch.
In analogy to Eq. (3), the switch contrast for stored gate
excitations is modeled by

\[
C(N_{g,st}) = 1 - \sum_{k=0}^{\infty} \frac{N_{g,st}^k e^{-N_{g,st}}}{k!} e^{-\text{min}(k,3) \cdot OD_{st}},
\]

We determine a mean optical depth \( OD_{st} = 2.2(7) \) per
stored gate excitation. This value results from the elongated
shape of our cloud, with gate excitations located in low
density regions reducing the average \( OD_{st} \) per excitation.
Longitudinal compression to \( a_l = r_{gs}/2 \) would increase
\( OD_{st} \) to the total optical depth of our system \[24\].

Next, we investigate how many source photons can be
switched by our system. To quantify the gate-induced
change in source transmission, we consider the optical
gain \( G = \frac{\bar{N}_{s,out}^{\text{no gate}}}{\bar{N}_{s,out}^{\text{with gate}}} \) \[12\]. In Fig. 3(a), we plot
the measured optical gain for an average input of gate photons
\( N_{g,in} = 0.75(3) \) and an increased integration time
\( t_{\text{int}} = 90 \mu s \), comparable to the fly-away time of stored
gate excitations (blue data points). For this gate input, we
observe a maximum optical gain \( G(N_{g,in} = 0.75) = 10(1) \).

Further increase of the optical gain at fixed gate input is
limited by the self-blockade of the source beam, which
results in nonlinear source transmission even in the absence
of gate photons \[18,19\]. The red [blue] data points in
Fig. 3(b) show the source photon transfer function when

\[
\bar{N}_{g,in} = 0 \text{ (green line)} \quad \text{and} \quad \bar{N}_{g,in} = 0.75(3) \text{ (blue line).}
\]

We observe a contrast switch between the two data sets over the whole source input range. The green [black] solid line are again the estimated behavior of the system for a single-photon Fock input state (a single stored excitation). Shaded regions are error estimates.

\[
C_{\text{coh},90 \mu s}(N_{g,in}) = \bar{N}_{g,in}^{75(3)}. \]

The saturation of transmitted photons even in the absence of gate photons is well described by the expression \( \bar{N}_{s,out} = a \cdot (1 - e^{-N_{g,in}/b}) \), where \( a \) is the maximum number of photons transmitted through the medium and \( b \) is the number of photons in the detection period where the self-nonlinear regime is reached \[24\]. Fitting this model to the data without gate input yields \( a = 46 \) and \( b = 70 \) [red line in Fig. 3(b)]. Repeating the
switch contrast analysis for low source input, we obtain
\( C_{\text{coh},90 \mu s} = 0.22(3) \) for the coherent gate input with
\( N_{g,in} = 0.75(3) \). Multiplying the self-nonlinearity fit with
\( (1 - C_{\text{coh},90 \mu s}) \) results in the blue line in Fig. 3(b), which is
in good agreement with the switched data points at all source photon inputs. From this we conclude that the stored gate excitations are unaffected by incoming source photon numbers as large as \( N_{s,in} \approx 250 \), showing that our Rydberg EIT transistor can achieve robust high optical gain \( G \gg 1 \) if the source photon loss due to self-blockade is overcome. One obvious improvement of our setup is to reach the longitudinal extent of the cloud, ideally to \( a_l = r_{gs}/2 \), while keeping the total OD constant. The resulting increased peak atomic density in our setup would not yet reach the fundamental limit set by Rydberg-ground state interaction \[24,30\]. Our two-color approach also offers the option of tuning the interstate interaction such that \( r_{gs} \gg r_{ss} \) by exploiting Stark-tuned two-color Förster resonances \[31,32\] or by directly working with dipole-coupled states.

Finally, the solid black (green) lines in Fig. 3(a) and 3(b)
show the expected optical gain and source transfer function
for a single photon Fock gate input (a deterministic single
stored Rydberg excitation). The mean optical depth
\( OD_{sp,90 \mu s} = 0.45(1) \) caused by a single photon Fock state
gate input and \( OD_{st,90 \mu s} = 0.94(10) \) caused by a single
stored excitation are obtained from fitting Eqs. (3) and (4)
to this data set. The reduction of mean optical depth stems from the fact that $t_{\text{int}} = 90 \mu$s is similar to the average fly-away time of the stored excitations. For a single excitation, we calculate the maximally achievable optical gain of our current system as $G_s = 28(2)$.

As a first application of our transistor we demonstrate single shot optical nondestructive detection of single Rydberg atoms in a dense background gas with high fidelity [26,27]. In Fig. 4(a) we show histograms of registered source photon events (not corrected for our photon detection efficiency of 0.31) obtained from many (250 each) individual runs of our transistor scheme for two different numbers of mean stored gate Rydberg excitations. For $N_{\text{stored}} = 0$ the histogram (blue bars) is Poissonian (solid blue line) within statistical errors. In contrast, the histogram recorded for $N_{\text{stored}} = 0.61(6)$ (red bars) shows a clearly non-Poissonian distribution with a strong redistribution towards zero detection events. Accounting again for the statistics of our classical gate pulses we can decompose the observed histogram into contributions with and without gate Rydberg excitations. The brown and orange histograms in Fig. 4(b) show the contributions of gated and not gated experiments to the measured red histogram. The gated subensemble consists mostly of runs with a single (73%) or two (22%) Rydberg excitation(s) in the cloud. A single gate excitation Fock state [33] would cause a very similar histogram due to the high switch contrast. The dashed green line shows the discrimination level for the decision in a single shot whether one or more Rydberg atoms were present or not [34]. From the decomposed histograms we calculate the fidelity of this prediction for the dataset shown in Fig. 4 to be $F = 0.72(4)$.

The limiting factor on the detection efficiency is again the self-blockade of the source photons, which prevents larger numbers of detection events for the nongated case. Possible improvements are similar to the one listed above for the transistor, if no spatial resolution of the detection is desired. For spatially resolved imaging of Rydberg ensembles [26,27], tuning of the interstate interaction is restricted, as $r_{gg}$ must remain smaller than half the distance between gate Rydberg atoms, given by $\sim r_{gg}/2$ in a blockaded ensemble, to prevent spatial blurring.

In summary, we have demonstrated a free-space single-photon transistor based on two-color Rydberg interaction. Further improvements of our system could enable a high optical gain, high efficiency optical transistor, so far only realized in a cavity QED setup [12]. One key issue we will address in the future is the retrieval of gate photon(s) after the switch process [21,24], which could enable multi-photon entanglement protocols and creation of nonclassical light-states with large photon numbers [35]. This requires the increase of the coherence time from its current value of $\sim 1 \mu$s by at least one order of magnitude. We have implemented optical nondestructive Rydberg atom detection at the single-particle level, which can be extended to spatially resolved imaging of Rydberg ensembles [26,27]. Increasing the gate photon storage efficiency would also enable high fidelity single photon detection [36], retrieval of the gate photon would make this scheme nondestructive [37]. Finally, our system is a highly sensitive probe for studying Rydberg interaction on the few-particle level [38]. In particular, the combination of two independently controlled Rydberg-EIT schemes enables novel fields of study, such as two-color Förster resonances [28,31,32], the interplay between slow light propagation and Rydberg exchange interaction [39], or realization of a two-photon phase gate based on Rydberg-polariton collision [25,40,41].

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FIG. 4 (color online). (a) Histograms of single shot detection events with and without stored gate excitation (red bars and blue bars, respectively). The strong shift of the red histogram originates from the switch effect of single or two gate Rydberg excitations in the medium. (b) Accounting for the Poissonian statistics of gate Rydberg excitations, we decompose the red histogram in (a) into gated and not-gated contributions. The dashed green line is the discrimination level which predicts the presence of a Rydberg atom in a single shot with the highest fidelity of 0.72(4).

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