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Electron and Nucleon Localization Functions of Oganesson: Approaching the Thomas-Fermi Limit

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Fermion localization functions are used to discuss electronic and nucleonic shell structure effects in the superheavy element oganesson, the heaviest element discovered to date. Spin-orbit splitting in the 7p electronic shell becomes so large (~10 eV) that Og is expected to show uniform-gas-like behavior in the valence region with a rather large dipole polarizability compared to the lighter rare gas elements. The nucleon localization in Og is also predicted to undergo a transition to the Thomas-Fermi gas behavior in the valence region. This effect, particularly strong for neutrons, is due to the high density of single-particle orbitals.

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Introduction.—Oganesson (Z = 118) is the recent addition to the periodic table of the elements and the chart of nuclides [1]. The isotope $^{294}_{118}$ Og was produced in a heavy ion fusion reaction with a $^{48}_{20}$ Ca beam and a $^{249}_{98}$ Cf target [2,3]. The heaviest element studied chemically to date is Fl (Z = 114). Its relatively long half-life, 1–2 s, enables chemical studies with ~5 atoms/day, which marks the limit of chemistry today [4,5]. The estimated α -decay halflife of $^{294}_{118}$ Og, $0.89^{+1.07}_{-0.31}$ ms, is too short for chemical "oneatom-at-a-time" studies; hence, its chemical properties must be inferred from advanced atomic calculations based on relativistic quantum theory [6–19]. According to these, Og has a closed-shell $[Rn]5f^{14}6d^{10}7s^27p^6$ configuration [13,20,21], with a very large spin-orbit splitting of the 7pshell (9.920 eV at the Dirac-Breit-Hartree-Fock and 10.125 eV at the Fock-space coupled-cluster level; see below). In contrast to its electronic configuration (Og completes the seventh period of the periodic table), it is not expected to behave like a typical rare gas of group 18. For example, the relativistic $7p_{3/2}$ expansion and the relativistic 8s contraction make Og the first rare gas element with a positive electron affinity of 0.064 eV [10,16,22]. This result includes a substantial quantum electrodynamic correction of 0.006 eV [16].

Nuclear structure calculations predict ²⁹⁴Og to be a deformed nucleus [23–26], eight neutrons away from the next neutron shell closure at ³⁰²Og (N = 184) [27–32]. A new factor impacting properties of superheavy nuclei is the strong electrostatic repulsion: The Coulomb force in superheavy nuclei cannot be treated as a small perturbation atop the dominating nuclear interaction; the resulting polarization effects due to Coulomb frustration are expected to influence significantly the proton and neutron

distributions and shell structure [26,28,31,33-37]. In particular, the isotope $^{294}_{118}$ Og is believed to be a semibubble system with a sizable central depression of the proton density [26].

The objective of this Letter is to study the electronic and nucleonic shell structure of superheavy elements. The electronic shell structure is expected to be impacted by the transition from the LS coupling of the Schrödinger equation at lower atomic numbers to the *j* i coupling of the Dirac equation at large Z values. In the nuclear case, the shell structure is expected to be washed out due to the large density of single-nucleonic states. While the kinematics of protons and neutrons in a nucleus is nonrelativistic, the large spin-orbit coupling (that is about an order of magnitude greater than in the atomic case due to large spindependent components of the nucleon-nucleon interaction [38]) results in a *jj* coupling. Therefore, for both electronic and nucleonic systems, the pattern of single-particle levels of superheavy species is expected to be strongly impacted by both radial and total angular momentum characteristics [39,40]. To describe these changes quantitatively, we utilize the fermion localization measure [41], which is an excellent indicator of shell structure. In particular, we investigate the transition from the regime of strong localization, governed by shell effects, to a more delocalized regime typical of a uniform-density Thomas-Fermi gas. As we shall demonstrate, superheavy species constitute an excellent territory to look for such a transition.

Fermion localization function.—The spatial localization measure was originally proposed in atomic and molecular physics to characterize shell structure and chemical bonding in electronic systems [41–47]. It has been subsequently introduced to nuclear physics to visualize cluster structures

in light nuclei [48]. The novel nuclear applications include a description of nuclear fission [49] and heavy-ion fusion [50] and nucleonic matter in the inner crust of neutron stars [51]. In electronic systems, the spatial localization function is referred to as the electron localization function (ELF), and in nuclear systems as the nucleon localization function (NLF). It is based on the inverse of the conditional probability of finding a fermion of type q (= e, n, or p)in the vicinity of another fermion of the same type and same spin or signature quantum number $\sigma (= \uparrow \text{ or } \downarrow)$, knowing that the latter particle is located at position r. While this probability is generally given by the nonlocal one-body density matrix [41], it is useful to introduce a local quantity that provides information about the short-range behavior. To this end, Becke and Edgecombe [41] introduced the local measure of fermion localization, which-in the nonrelativistic case-can be written as

$$C_{q\sigma}(\mathbf{r}) = \left[1 + \left(\frac{\tau_{q\sigma}\rho_{q\sigma} - \frac{1}{4}|\nabla\rho_{q\sigma}|^2 - \mathbf{j}_{q\sigma}^2}{\rho_{q\sigma}\tau_{q\sigma}^{\mathrm{TF}}}\right)^2\right]^{-1}, \quad (1)$$

where $\rho_{q\sigma}$, $\tau_{q\sigma}$, $j_{q\sigma}$, and $\nabla \rho_{q\sigma}$ are the particle density, kinetic energy density, current density, and density gradient, respectively. $\tau_{q\sigma}^{\text{TF}}$ denotes the Thomas-Fermi kinetic energy. In this work, time reversal symmetry is conserved; hence, $j_{q\sigma}$ vanishes.

The localization function takes generally values between 0 and 1. A value close to 1 indicates that the probability of finding two particles (of the same type) close to each other is very low. Thus, a high value of C marks the spatial regions corresponding to shell separations. Since the localization function (1) is normalized to the Thomas-Fermi kinetic energy, C = 1/2 corresponds to the limit of the uniform-density Fermi gas, in which the individual orbits are spatially delocalized.

Electron localization.—For the electronic structure calculations, we used the ELF module as implemented in the relativistic ab initio quantum chemistry program DIRAC15 [52]. Hartree-Fock one-particle densities were generated in nonrelativistic, scalar-relativistic (module x2C-spinfree) [53,54], and (four-component) Dirac-Coulomb calculations in conjunction with an uncontracted relativistic quadruplezeta basis set DYALL.ACV4Z [55]. The Dirac-Fock computations include the small-component integrals as well as the two-electron Gaunt term. We utilized the finite-field method to compute the static electric dipole polarizability of Og (with external electric field strengths of 0.0, 0.0005, and 0.001 a.u.) at the CCSD(T) coupled-cluster level [12], which included excitations from singles, doubles, and perturbative triples. In the correlation treatment, we included 50 electrons and virtual orbitals up to 25 a.u. Here we used the molecular meanfield x2C Hamiltonian [56] with the Gaunt term included. Fock-space coupled-cluster calculations [16] were carried out to obtain the ionization potentials from the filled $7p_{3/2}$ and $7p_{1/2}$ shells of Og. Note that only large-component densities are considered for the nonrelativistic and scalarrelativistic ELF, whereas in the four-component case the small-component densities are added to the large components to yield the total one-particle density. Relativistic effects make a huge imprint on many properties of Og. For instance, the electron binding energy of Og is predicted to rise by as much as 227 keV by considering relativistic effects (for comparison, a similar number for Pb is a mere 40 keV).

Figures 1 and 2 show the ELFs predicted in our calculations. As seen in Fig. 1, electron localizations for Xe or Rn hardly change from the nonrelativistic to the fourcomponent relativistic framework. However, for Og we see significant electron delocalization with ELF values that are much smaller compared to the nonrelativistic case, making the atomic shell structure barely recognizable. The pattern of concentric rings is a fingerprint of the underlying shell structure. The sizes of rings in the ELF reflect the radii of electron orbits in different shells; hence, they roughly scale with n^2 , where *n* is the principal quantum number [41,42]. Figure 2(b) clearly shows that the delocalization is mainly due to spin-orbit coupling and not due to scalar-relativistic effects. This results in an evenly distributed ELF with values around 0.5 in the outer shells. The valence and subvalence shells of Og are, therefore, smeared out like in a homogenous electron gas. Rn behaves similarly to Xe, although some delocalization through relativistic effects is already apparent.



FIG. 1. ELFs from nonrelativistic (NR, left) and Dirac-Hartree-Fock calculations (R, right) for the heavy rare gas atoms Xe (top), Rn (middle), and Og (bottom).



FIG. 2. ELFs for Xe (a) and Og (b) from nonrelativistic (NR), scalar-relativistic (SR), and Dirac-Hartree-Fock (R) calculations as a function of the distance from the nucleus as in Ref. [41]. The relativistic contraction of inner shells and smearing out of the shell structure in the valence and subvalence shells of Og are clearly seen.

A more detailed analysis shows that smearing out of the electron density in the valence region originates from the strong spin-orbit splitting of the 7p shells; while the radii for the valence 5p orbitals in Xe are very similar (2.239 and 2.141 a.u. for $5p_{3/2}$ and $5p_{1/2}$, respectively, as obtained with the numerical program GRASP92 [57]), the $7p_{3/2}$ shell in Og is 0.75 a.u. further out compared to the $7p_{1/2}$ shell (2.796 and 2.039 a.u., respectively). Large spin-orbit splittings are also calculated for the lower-lying $\ell > 0$ (core) shells. Furthermore, the density of the single-particle (SP) states increases from Xe to Og as expected for higher principal quantum numbers; see Fig. 3. As a result of these effects, the electron density is more homogeneously distributed over the entire atomic range, i.e., less localized, resulting in ELF values oscillating around the Thomas-Fermi limit. Our Fock-space coupled-cluster calculation gave ionization potentials of $7p_{3/2}$ and $7p_{1/2}$ of 8.842 and 18.967 eV, respectively; thus, spin-orbit splitting for the valence 7p orbital of Og is extremely large (10.125 eV). Figure 3 illustrates this in relation to the orbital energy levels of the lighter homologues.

According to the Thomas-Fermi model, the static dipole polarizability $\alpha \propto r_a^3$, with r_a^3 being the atomic radius [58]. Our state-of-the-art calculations show that the electron-gas-like outer shell of Og, resulting in $\alpha = 57.98$ a.u., is much easier to polarize as compared to xenon ($\alpha = 27.815$ a.u. [59]) or radon ($\alpha = 33.18$ a.u. [60]). For comparison, the nonrelativistic and scalar-relativistic values for Og are



FIG. 3. Orbital energy levels of Xe (left), Rn (middle), and Og (right) for the ${}^{1}S_{0}$ ground state as obtained from nonrelativistic (NR) and scalar-relativistic (SR) Hartree-Fock and Dirac-Hartree-Fock (R) calculations. 6*s* (Xe), 7*s* (Rn), and 8*s* (Og) orbital energies are taken from the first excited ${}^{3}P_{2}$ state.

 $\alpha = 45.30$ a.u. and $\alpha = 43.78$ a.u., respectively. Thus, for Og one expects an increase in van der Waals interactions compared to the lighter rare gases and, subsequently, a significant change in the chemical and physical properties of this element; see also Refs. [10–12,15,19,61] for more discussion on this point.

Nucleon localization.—For the nuclear calculations, we employ the nuclear density functional theory (DFT) [62] with carefully optimized global Skyrme energy density functionals UNEDF1 [63] and SV-min [64]. Pairing is of minor importance in the closed-shell nuclei considered. It is treated as in Ref. [26]. Namely, we consider the densitydependent contact force at the level of the BCS theory. The pairing space is limited by a soft cutoff with the cutoff parameter chosen such that it covers about 1.6 extra oscillator shells above the Fermi energy. We use the DFT solver of Ref. [65] constrained to spherical geometry, as all nuclei considered are expected to be spherical in their ground states.

Figure 4 shows the NLFs for the doubly magic mediummass nucleus ¹³²Sn and spherical superheavy systems ³⁰²Og and ⁴⁷²164. We consider the latter "theoretical" nucleus to further illustrate the behavior of NLFs at still larger numbers of nucleons. In contrast to the ELFs, the number of closed shells cannot be determined from the number of radial maxima. This is due to the different radial behavior of single-nucleon orbits. While the radii of electron orbits in atoms belonging to different shells are spatially well separated, the radii of nucleonic orbits scale roughly as $\sim \sqrt{2n_r + \ell}$; i.e., they very gradually increase with the shell number. This results in a large spatial overlap between single-nucleon wave functions and reduced localizations as compared to the electronic case. A characteristic feature of



FIG. 4. NLFs of ¹³²Sn, ³⁰²Og, and ⁴⁷²164 calculated with the energy density functional UNEDF1.

NLFs is the local enhancement at the surface [49] due to the fact that few valence nucleons contribute to the total density at distances greater than the nuclear radius.

Inspecting the NLFs of protons to neutrons, one notes that the patterns of concentric rings are more distinct in the proton system, as the number of occupied proton shells is less than that for the neutrons, within the same volume (as the rms proton and neutron radii are very similar [24]). This effect becomes fairly pronounced for superheavy nuclei where the neutron excess is large. While the NLF for the medium-mass nucleus ¹³²Sn exhibits a clear shell structure with distinct oscillations around C = 0.5 [49], the maxima and minima become fainter for heavier systems. This is particularly striking for the neutrons. While the neutron NLF for ³⁰²Og still exhibits a faint structure in the interior, the ring pattern almost vanishes for ⁴⁷²164. Overall, as the mass increases, the neutron localization approaches the Thomas-Fermi limit C = 0.5 in the valence region (r > 3 fm) below the surface peak. The NLF pattern seen in Fig. 4 reflects the underlying nucleonic shell structure. As discussed in, e.g., Refs. [27-32], the general pattern of SP energies undergoes significant changes in superheavy nuclei. First, the SP level density is large; in fact, it grows faster than $A^{1/3}$ [32]. Consequently—similar to what has been discussed earlier in the context of atomic calculations of the electron shell structure of superheavy elementssmall changes in the theoretical description can impact the shell structure substantially. Second, the shell structure of superheavy nuclei is influenced by the self-consistent interplay between the short-range attractive nuclear force and the long-range electrostatic repulsion. Thanks to the resulting Coulomb frustration, significant rearrangements of nucleonic densities, such as the appearance of central depression, are predicted [26,28,31,33–37]. The presence of central depression strongly affects high-*j* orbits due to their large SP radii [27,31,34,36].

Conclusions.—To study electronic and nucleonic shell structure in superheavy elements, we employed the local spatial measure of fermion localization. The atomic calculations were carried out for heavy rare gas atoms Xe, Rn, and the superheavy element Og recently added to the periodic table. The nuclear calculations were performed for the known doubly magic system ¹³²Sn and for superheavy nuclei ³⁰²Og, and ⁴⁷²164. This study constitutes the first application of fermion localization to superheavy atoms and nuclei.

Relativistic effects significantly impact the electronic structure of superheavy atoms. For the element Og, the electron shells with $\ell > 0$ show very large spin-orbit splittings smearing out of the one-particle density, thus becoming more uniformly distributed over the entire atom approaching the electron-gas regime in the valence region. A direct consequence of this transition is its predicted large static dipole polarizability resulting in an increase in van der Waals interactions compared to the lighter rare gases and a significant change in its chemical and physical properties.

A gradual transition towards the uniform-gas regime is predicted for nucleonic localizations in superheavy nuclei. In general, neutrons are more delocalized than protons; as for the superheavy nuclei N is much greater than Z; i.e., more neutrons are confined to the same volume than protons. While the semiclassical Thomas-Fermi limit in nuclei is strictly approached only for systems with extremely large particle numbers A > 5000 [40,66,67], we can see that in the discussed superheavy nuclei the Fermi-gas limit of neutron NLFs is reached in the valence region (r > 3 fm) below the surface peak.

In summary, through electron and nucleon localization functions we show that Og is a rather unusual addition to the periodic table and to the chart of nuclides. A high density of electronic and nucleonic SP states, relativistic effects resulting in the strong spin-orbit splitting of electronic levels, and nucleonic polarization effects make the superheavy atoms, such as Og, quantitatively different from the lighter congeners.

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Correction: The previously published Figure 2 contained an error in the axis label and has been replaced.