Lawson Criterion for Ignition Exceeded in an Inertial Fusion Experiment

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For more than half a century, researchers around the world have been engaged in attempts to achieve fusion ignition as a proof of principle of various fusion concepts. Following the Lawson criterion, an ignited plasma is one where the fusion heating power is high enough to overcome all the physical processes that cool the fusion plasma, creating a positive thermodynamic feedback loop with rapidly increasing temperature. In inertially confined fusion, ignition is a state where the fusion plasma can begin “burn propagation” into surrounding cold fuel, enabling the possibility of high energy gain. While “scientific breakeven” (i.e., unity target gain) has not yet been achieved (here target gain is 0.72, 1.37 MJ of fusion for 1.92 MJ of laser energy), this Letter reports the first controlled fusion experiment, using laser indirect drive, on the National Ignition Facility to produce capsule gain (here 5.8) and reach ignition by nine different formulations of the Lawson criterion.

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Nuclear fusion reactions combine two light nuclei into a heavier one, releasing substantial energy in the process. Approaches to generating energy production from fusion typically use thermal reactions (where electron temperature $T_e$ and ion temperature $T_i$ are similar); in order for copious reactions to occur the fuel must be at extremely high ion temperatures, on the order of several kilo-electron-volts (where 1 keV = $1.16 \times 10^7$ K). The fundamental challenge of fusion is that while the fusion reactions can self-heat the plasma, at these temperatures the plasma also rapidly loses energy via cooling mechanisms, such as the x-ray radiation that is emitted by the bremsstrahlung process. Early researchers recognized that the most favored fusion reaction is deuterium (D)–tritium (T) fusion [D + T → n(14.1 MeV) + 4He(3.5 MeV)] [1] because it has the lowest temperature, $\approx 4.3$ keV, at which fusion self-heating power just balances losses from bremsstrahlung x-ray radiation. Additional energy loss mechanisms, such as heat conduction, also cool the plasma, requiring higher temperatures than 4.3 keV to achieve “ignition,” which is when the self-heating overpowers all loss mechanisms (“Lawson-like” ignition criteria) [2] and the temperature rises through a positive thermodynamic instability, resulting in an increasing fusion burn. Such conditions occur in nature in novae and type-Ia supernovae, or terrestrially in thermonuclear weapon explosions. Ignition is a step beyond a “burning plasma,” where self-heating exceeds the external energy input to heat the plasma as had been recently achieved [3,4]. This Letter reports on the culmination of a decade effort in inertial confinement fusion (ICF) on the National Ignition Facility (NIF) [5] that resulted in an igniting implosion with over a megajoule fusion yield putting ICF on the threshold of unity gain in the laboratory for the first time. This is the first controlled fusion experiment to exceed Lawson-like ignition statements.

Ignition is required for net gain and energy applications using the ICF approach; in contrast, ignition may not be required for other approaches to fusion such as magnetic confinement experiments like the ITER experiment [6]. The original idea behind ICF was explored using lasers to focus energy onto a small capsule containing DT fuel and isentropically compress the target to obtain high thermal temperature ($T_{th} \approx T_e \approx T_i$) and pressures [7,8] (see Ref. [9] for the early history). Here, the fusion burn proceeds while contained by the inertia of the fuel itself over a brief period of time. The inertial confinement time ($\tau$) is related to the “areal density” [$\rho R$ as the radial integral of density, $\rho(R)$] of the fuel. Ignition and subsequent burn into the surrounding fuel (burn propagation) initiates an explosive, but microscopic scale, release of energy.

Instead of directly driving a capsule with lasers, as originally proposed, here we use “indirect drive.” The indirect-drive approach to ICF [10] drives a high atomic number cavity, a hohlraum [see Fig. 1(a)], with laser energy, thereby generating a bath of intense x rays, measured in terms of radiation temperature [$T_{rad} \sim 300$ eV, see Fig. 1(b)]. The capsule placed at the center of the hohlraum [see Fig. 1(a)] and its outer surface, the ablator, absorbs the x-ray energy (roughly in proportion to the surface area ratio of the capsule to hohlraum) in a thin layer of ionized plasma, generating high ablation pressures (of order hundreds of megabars) which produces an inward acceleration (implosion) that accelerates the remaining ablator and DT fuel to high velocity. The generation of ablation pressure is accompanied...
by the generation of inwardly directed shock waves [11], the precise control of which are a key aspect of any modern ICF design [12–15].

The key element of any ICF scheme is the implosion. Implosions are hydrodynamic systems that do mechanical $pdV$ work on the fusion fuel to both compress and heat it to a high energy-density state, triggering thermonuclear reactions. As the fuel implodes at high velocity ($v_{\text{imp}}$) inwardly, the central pressure begins to increase as the fuel decelerates, doing mechanical work in a process termed “stagnation.” During stagnation, the implosion kinetic energy is converted into internal energy, increasing the temperature and pressure ($p \approx 0.77 \rho T_{\text{th}}$ in gigabar, g/cm$^3$, and kilo-electron-volt units) in the DT fuel. In “hot spot ignition” [21] only a small fraction of the total DT fuel ($\sim 1/10$) is initially heated, reducing the internal energy needed to reach the required $T_{\text{th}}$ for ignition.

While the NIF can deliver up to 1.9 MJ of laser energy [5,22–24] in frequency tripled (351 nm) light to the hohlraum, typically only $\sim 20$ kJ is converted to fuel kinetic energy because of the inherent inefficiency of the indirect drive approach [10,15,25,26]. This limited energy results in requiring $t_{\text{imp}} \sim 400$ km/s and pressures of hundreds of gigabars [27] to reach the $T_{\text{th}}$ and $\rho R$ required to initiate substantial self-heating in the central hot spot through deposition of the fusion reaction products ($\alpha$ particles, $\text{He}^3$, and $\text{He}^4$).

FIG. 1. (a) Cutaway characteristic target geometry (gold-lined depleted uranium hohlraum surrounding an HDC capsule) with some features labeled. The capsule, $\sim 2$ mm diameter, at the center of the hohlraum, $\sim 1$ cm height, occupies a small fraction of the volume. Laser beams (not shown) enter the target at the top and bottom apertures called laser entrance holes (LEH’s) (outer beams: 44° and 50°, inner beams: 23° and 30° relative to the vertical axis of symmetry). The LEH washer forms the LEH aperture. The “starburst” allows imaging of the DT fuel layer during experiment preparation as cryogenic DT liquid is flowed into the capsule via the “fill tube.” (b) Total laser power (blue) vs time and simulated [16] hohlraum radiation temperature ($T_{\text{rad}}$) (red) vs time for experiment N210808 are shown with a few key elements, discussed in the text, labeled. The “picket” of the laser pulse delivers the first significant burst of energy to the hohlraum and is key to controlling implosion compressibility and hydrodynamic stability. The “foot” of the laser pulse is the duration of the pulse before the rise to peak power—it sets the entropy of the DT fuel via a series of shock waves. The capsule ablation pressure is directly related to $T_{\text{rad}}$ and the ablator composition (which in this case is high density carbon, HDC). A key aspect shown is the laser typically turns off $\approx 1$ ns before bang time (denoted “coast-time” duration), of order the hohlraum cooling time [17]. Increasing late-time x-ray drive results in reduced coast time which enhances the conversion of implosion kinetic energy to DT internal energy [18,19]. (c) Imaging data from experiments: neutron images [20] are taken at three lines of sight: (0,0) (technically at $\theta = 5.75$ and $\phi = 225$), (90,213), and (90,213) in target-chamber coordinates ($\theta, \phi$) are the respective polar and azimuthal angles measured from the top looking down of the NIF target chamber in degrees]. All images are 100 $\mu$m square. Imaging data are used to reconstruct the hot spot plasma volume needed for inferring pressure and other plasma properties.
which are the $^4\text{He}$ nuclei). Designing an implosion that satisfies these conditions, while also controlling hydrodynamic instability (a consequence of the tremendous accelerations and decelerations, $\sim 10^{14-15}$ m/s$^2$, and material density gradients involved in the implosion) \cite{28} and asymmetry \cite{29-34}, requires finesse and engineering control.

Hydrodynamic instability \cite{35-37} can lead to mixing of higher Z (atomic number) capsule ablator material into the fuel and eventually the hot spot, reducing the ion temperature through radiative cooling \cite{38,39} that raises the threshold for ignition \cite{40}. Instability can be seeded by fabrication defects on the capsule \cite{41}, and by engineering structures such as the support “tent” membrane [see Fig. 1(a)] that holds the capsule in the center of the hohlraum [42-44] and a 2–10 μm diameter glass tube [45–49] that is inserted into the capsule to fill it with DT fuel. The latter results in a hydrodynamic jet of ablator material entrained into the hot spot resulting in additional radiative cooling [50–52]. Thicker capsules and DT fuel layers are expected to reduce the mixing into the hot spot \cite{53}, but this choice lowers the maximum possible implosion velocity, with fixed drive, due to the extra mass. So, with limited laser power and energy available, a more efficient hohlraum \cite{4,53,54} is needed to recover implosion velocity.

The NIF commenced layered DT experiments in June 2011 with very high convergence “low-foot” designs using plastic capsules in a high gas fill (i.e., helium gas fills of $\geq 0.96$ mg/cm$^3$) hohlraum \cite{15} (see Appendix A for a more complete history of key experiments). The 2011–2012 experiments were impacted by high laser-plasma instability (LPI) leading to implosion asymmetry and were more impacted by hydrodynamic instabilities than expected. Stability was improved by using a higher adiabat (i.e., higher DT fuel entropy) three-shock [see Fig. 1(b)] high-foot design \cite{28,55} by raising the power in the “foot” (the first 3–4 ns period before the rise to peak power) of the laser pulse—a tactic that is still used presently [see Fig. 1(b)]. The high foot accessed higher $v_{\text{imp}}$, higher $I_{\text{th}}$, and higher fusion yields with significant $\alpha$-particle self-heating \cite{56,57} by systematically reducing coast time thereby increasing late-time ablation pressure [e.g., see Fig. 1(b)], but asymmetry and the reemergence of instability as $v_{\text{imp}} \sim 390$ km/s was approached capped performance. High-foot designs used the same hohlraum as the low foot, albeit with an even higher helium gas fill of 1.6 mg/cm$^3$ and suffered from similar hohlraum problems. A parallel effort exploring exploding pushers in near vacuum hohlraums, for neutron diagnostic flat fielding, mitigated losses due to LPI leading to a transition away from high gas-fill hohlraums \cite{58,59}. Without a high gas fill, the hohlraum needed to be larger in diameter to delay the ingress of hohlraum plasma into the path of the laser beams. HDC (“high density carbon,” i.e., industrial diamond) ablators, which are relatively thinner than plastic (for fixed capsule mass because of the density difference of 3.3–3.5 g/cm$^3$ for HDC vs 1.05 g/cm$^3$ for plastic), allowed for shorter laser pulses which also reduced the ingress of hohlraum plasma. Implosion designs using HDC ablators seemed to tolerate the hydrodynamic perturbations from the tent membrane [a 45 nm thick Formvar film that holds the capsule in the center of the hohlraum as shown in Fig. 1(a)], but are more susceptible to hydrodynamic perturbations from the fill tube [again see Fig. 1(a)], motivating an engineering effort to reduce the fill tube diameter. Observed limits \cite{60} on convergence levels with HDC based ablators motivated an alternate strategy using larger capsules to increase energy coupled to the hot spot while not reducing stagnation pressure. With facility limits on maximum laser energy, a simple hydroscale of all physical dimensions would lead to less x-ray drive resulting in the capsule velocity decreasing and coast for a longer duration, decompressing before stagnation resulting in poor conversion of kinetic energy to hot spot internal energy. Thus, the capsule radius was increased, but the thickness was not increased in the same proportion in order to maintain $v_{\text{imp}}$—this was the HYBRID strategy \cite{61-63}.

An engineering surprise was apparent when larger radius HDC capsules were first manufactured, exhibiting voids inside the bulk of the shell and pits on the surface of the shell, a problem that challenged an early HYBRID design \cite{64,65} and is still an engineering problem today. Along with laser improvements (see Appendix B), advances in the understanding of symmetry control in low gas-fill hohlraums, namely an empirical model \cite{66} and extension of cross-beam energy transfer (CBET) tuning to low gas-filled hohlraums through wavelength detuning \cite{67} enabled increasing the capsule scale in more efficient hohlraums.

This Letter reports on work using the HYBRID-E \cite{4,53,54} design which increased the amount of energy delivered to the “hot spot” by increasing the capsule radius by 15% compared to previous experiments \cite{64,68-70}. The challenge of increasing initial capsule radius with fixed laser drive is the potential loss of energy density at the core of the implosion \cite{71}. It is therefore essential to, while increasing the size, maintain the other implosion design parameters including the compressibility of the fuel (“adiabat”), $v_{\text{imp}}$, and the late-time ablation pressure from the drive \cite{18}.

In experiment N210808 (notation being NYYMMD, \(N = \text{NIF}, \ YY = \text{year}, \ MM = \text{month}, \ DD = \text{day}\)) that is the focus of this Letter, the late-time ablation pressure was further increased, motivated by a design study which suggested a further improvement in hot spot pressure could be achieved for the HYBRID-E design relative to the previously reported experiments (N210207 and N210307) \cite{3,4} through changes made to the hohlraum radiation drive as described in Kritcher \textit{et al.} \cite{16}. In addition, the hydrodynamic stability of the design and the quality of the diamond ablator were both improved.
Hohlraum efficiency was improved by ~15% reducing the diameter of one of the main sources of radiation loss, the laser-entrance holes (LEH) on both ends of the hohlraum [see Fig. 1(a)]. The reduced LEH diameter was first tested using a gas-filled capsule nonignition experiment N210601 [72,73], which verified improved energy coupling with adequate low-mode symmetry. A more efficient hohlraum requires less peak laser power to maintain $T_{\text{rad}}$ during most of the laser pulse, and the Saved energy was used to extend peak laser power increasing late-time ablation pressure [see Fig. 1(b)]. In-flight implosion radiography data [74] showed that reducing coast time [75,76] does significantly increase peak $v_{\text{imp}}$ and, per theory [18,19], stagnation pressure by maintaining higher late-time ablation pressure.

Radiation hydrodynamic simulations (HYDRA [77], which itself uses detailed equations of state [78,79], transport [80,81], electron-ion coupling [82,83] and opacity models [84]) was used to calculate these design modifications [16]. The mode-1 radiation flux asymmetry from the hohlraum [see Fig. 1(a)]. The reduced LEH diameter of one of the main sources of radiation loss, the laser-entrance holes (LEH) on both ends of the capsule, estimated from postshot simulations), target gain (ratio of yield to x-ray energy absorbed by the capsule, estimated from postshot simulations), target gain (ratio of yield to mechanical energy delivered to the DT), capsule gain (ratio of yield to x-ray energy absorbed by the capsule, estimated from postshot simulations), target gain (ratio of yield to laser energy delivered to the target).

<table>
<thead>
<tr>
<th>Quantity</th>
<th>N210207_Data</th>
<th>N210307_Data</th>
<th>N210808_Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_{\text{DT}}$ (keV)</td>
<td>5.66±0.13</td>
<td>5.55±0.11</td>
<td>10.9±0.4</td>
</tr>
<tr>
<td>$T_{\text{DD}}$ (keV)</td>
<td>5.23±0.16</td>
<td>4.87±0.14</td>
<td>8.94±0.4</td>
</tr>
<tr>
<td>DSR (%)</td>
<td>3.16±0.16</td>
<td>3.49±0.16</td>
<td>2.87±0.24</td>
</tr>
<tr>
<td>$V$ (10$^4$μm$^3$)</td>
<td>3.3±0.3</td>
<td>2.7±0.3</td>
<td>6.4±0.75</td>
</tr>
<tr>
<td>$\tau_{\text{FW}}$ (ps)</td>
<td>103±25</td>
<td>138±20</td>
<td>89±5</td>
</tr>
<tr>
<td>$p_{\text{HS}}$ (Gbar)</td>
<td>351±23</td>
<td>353±23</td>
<td>569±61</td>
</tr>
<tr>
<td>$E_{\text{HS}}$ (kJ)</td>
<td>17.4±1.1</td>
<td>14.6±0.9</td>
<td>55±6</td>
</tr>
<tr>
<td>$\rho_{\text{HS}}$ (g/cm$^2$)</td>
<td>0.37±0.4</td>
<td>0.38±0.02</td>
<td>0.44±0.05</td>
</tr>
<tr>
<td>$G_{\text{fuel}}$</td>
<td>7.5$^{+0.54}_{-0.82}$</td>
<td>7.77$^{+0.55}_{-0.82}$</td>
<td>75.6$^{+3.6}_{-5.6}$</td>
</tr>
<tr>
<td>$G_{\text{capsule}}$</td>
<td>0.75±0.05</td>
<td>0.69±0.05</td>
<td>5.8</td>
</tr>
<tr>
<td>$G_{\text{target}}$</td>
<td>0.089</td>
<td>0.075</td>
<td>0.72</td>
</tr>
</tbody>
</table>
Once this tipping point, ignition, is reached thermal instability follows and $T_{th}$ increases in a finite-time singular (explosive) fashion over the “bootstrapping” timescale, dimensionally determined per Eq. (1) by the ratio of heat capacity and $\alpha$ heating rate at stagnation (subscript $s$) namely, $dt/d \ln T_{th} \sim c_{DT} T_{th}/(f_\alpha Q_\alpha) \sim 2.9 \times 10^{-5} c_{DT}/(f_\alpha \rho R T_{s}^{2.6}) \sim 0.8's$ of ps. Since ICF implosions are dynamic, thermodynamic instability is eventually terminated by expansion as the system blows itself apart.

Here, ignition in a fusion plasma is a statement about power balance, as it has been historically [2], and many works have generated criteria to estimate crossing this threshold in the ICF context [99–107], a context that Lawson’s 1957 work only speculated about. Conceptually simpler, “gain” is a statement about energy thresholds. Since ICF has many stages of concentrating energy at successively smaller volumes, a number of definitions of gain are commonly used. Namely, target gain (or just gain), $G_{target} = Y_{tot}/E_{las}$ is the ratio of total fusion yield ($Y_{tot}$) to laser energy input to the target ($E_{las}$), capsule gain, $G_{cap} = Y_{tot}/E_{abs}$, which compares the yield to capsule absorbed energy, and fuel (or DT) gain, $G_{fuel} = Y_{tot}/E_{fuel}$, compares the yield to the energy absorbed into the DT fuel [108]. Note that $G_{target} > 1$ does not imply net energy gain from a practical fusion energy perspective because the energy consumed by the laser facility is considerably larger than $E_{las}$. The terms ignition and target gain have sometimes been conflated [109] for simplicity, because the impulsive nature of an implosion can complicate the assessment of the power balance near the tipping point of ignition and the methods to do so (described below) were not developed until the past decade.

Herein gain values, $G_{target}$, $G_{cap}$, and $G_{fuel}$ (Table I) and ignition metrics (Table II) are calculated for the NIF experiment N210808 (and database of preceding shots). The processes of $\alpha$ heating can significantly modify hot spot properties, as a result some ignition metrics are phrased in terms of “$\alpha$-off” (also known as no-$\alpha$) properties [101,102,110], which represent the inferred plasma properties as additional fuel is ablated into the hot spot, all resulting in an amplification of fusion yield ($Y_{amp}$, the factor by which the yield increases above what $pdV$ work alone would have produced). Generally, stopping 14 MeV fusion neutrons is not possible in an ICF hot spot, so it is only the stopping of the $\alpha$ particles that matters. The quantity $f_\alpha \leq 1$ in Eq. (1) is the fraction of $\alpha$ particles stopped in the hot DT plasma and is related to the $T_{th}$ and $\rho R$ dependent $\alpha$-stopping distance for which a number of different approximations exist [98]; typical values are $f_\alpha \sim 0.7–0.8$. The $pdV$ work term in Eq. (1), is a source of mechanical power injection into the plasma on implosion $(dV/dt < 0)$ or a loss term upon explosion $(dV/dt > 0)$ as the volume $V$ surrounding the hot plasma changes.

A tipping point in DT plasma self-heating can be obtained if the $f_\alpha Q_\alpha$ term in Eq. (1) dominates over the other terms on the right-hand side of the power balance for sufficient time. Models of the hot spot energy partition for N210808, Fig. 2, show that the amount of $\alpha$ heating energy in the hot spot far outweighs the amount of $pdV$ work done on the hot spot and the loss terms (Bremsstrahlung radiation loss and conduction loss), resulting in a significant increase in hot spot internal energy well beyond the time of explosion (when the $pdV$ power changes sign). Once this tipping point, ignition, is reached thermal

![Graph](image_url)

**FIG. 2.** Simulated hot spot powers of Eq. (1) as a function of time from a model of N210808 [16]. Note that the negative $pdV$ rate of work is a loss comparable to the radiation loss and exceeds the conduction loss, even before peak $\alpha$-heating power is obtained, which is why satisfying the self-heating condition, $f_\alpha Q_\alpha > f_\beta Q_{B,DT} + Q_{\alpha}$, is necessary but not sufficient for determining ignition of an ICF implosion. After the time of peak $\alpha$-heating power the negative $pdV$ work is the dominant power loss.

#### Table II. Likelihood of N210808 surpassing several scientific metrics developed for ignition in inertial fusion.

<table>
<thead>
<tr>
<th>Metric</th>
<th>N210207</th>
<th>N210307</th>
<th>N210808</th>
</tr>
</thead>
<tbody>
<tr>
<td>GLC$_L$</td>
<td>0%</td>
<td>0%</td>
<td>99.6%</td>
</tr>
<tr>
<td>GLC$_\beta$</td>
<td>0%</td>
<td>0%</td>
<td>100%</td>
</tr>
<tr>
<td>($E_{\alpha}/2E_{fus}$) (0D)</td>
<td>0%</td>
<td>0%</td>
<td>100%</td>
</tr>
<tr>
<td>($E_{\alpha}/2E_{fus}$) (1D)</td>
<td>0%</td>
<td>0%</td>
<td>99.8%</td>
</tr>
<tr>
<td>ITFX$_{\alpha-off}$</td>
<td>0%</td>
<td>0%</td>
<td>100%</td>
</tr>
<tr>
<td>Cheng</td>
<td>0%</td>
<td>0%</td>
<td>100%</td>
</tr>
<tr>
<td>Tipton</td>
<td>6.2%</td>
<td>0%</td>
<td>100%</td>
</tr>
<tr>
<td>Atzeni</td>
<td>100%</td>
<td>100%</td>
<td>100%</td>
</tr>
<tr>
<td>Coutant</td>
<td>0%</td>
<td>0%</td>
<td>100%</td>
</tr>
<tr>
<td>$dT^2/dt &gt; 0$</td>
<td>No</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>NAS 1997</td>
<td>No</td>
<td>No</td>
<td>No</td>
</tr>
</tbody>
</table>
conditions that would be present in the implosion if α heating did not occur. The value of α-off metrics lies in their ability to identify the presence of an ignition cliff whereby small incremental changes in the metric result in large shifts in fusion yield as a result of α heating. In order to use no-α conditions, a model is used to translate measured properties into inferred no-α properties, which introduces a model uncertainty into the assessment. Alternatively, some ignition metrics are developed to directly use measured “α-on” properties, avoiding an intermediate model translation, but these also have uncertainty due to the feedback of α heating on the plasma properties used in the metric which the underlying theory attempts to account for. In this assessment, a suite of both α-on and no-α ignition metric types are utilized based upon the data from Table 1.

Based upon a definition of ignition as doubling of the hot spot temperature due to α heating, which corresponds to $Y_{\text{amp}} \approx 30$, Lindl et al. [106] derive both α-on and no-α ignition metrics for one-dimensional (1D) x-ray driven ICF targets and calibrate the model to simulations. Lindl’s model emphasizes the effect of ablating remaining mass and kinetic energy on the ignition metric, and a useful α-on ignition metric, a generalized Lawson criterion, GLC$_L$, that can be compared to data-inferred quantities is obtained

$$ \text{GLC}_L = \frac{\bar{P}_{\text{HS}}}{420 \text{ Gbar}} \times \frac{\bar{R}_{\text{HS}}}{50 \mu m}, \quad (2) $$

where GLC$_L > 1$ determines ignition. Lindl et al. utilizes quantities for pressure and radius that are burn weighted in both time and space. We denote these time-averaged quantities $\bar{P}_{\text{HS}}$ and $\bar{R}_{\text{HS}}$ to distinguish them from the main inferences in this Letter, which are the spatially burn-weighted quantities at peak burn. The time-averaged pressure is inferred using the prescription in Ref. [94]. The radius defined in Ref. [106] is larger than the radius determined from neutron data (i.e., Table 1) and we adjust the value using relations given in Ref. [106]. As shown in Fig. 3, unlike all previous shots on NIF, N210808 ignited the value using relations given in Ref. [106]. As shown in Fig. 3, unlike all previous shots on NIF, N210808 ignited the value using relations given in Ref. [106].

![Image](https://via.placeholder.com/150)

**FIG. 3.** NIF DT shot data (symbols) are plotted in the space of time-averaged inferred hot spot pressure ($\bar{P}_{\text{HS}}$) and hot spot radius ($\bar{R}_{\text{HS}}$). The black dashed curve denotes the ignition boundary from Eq. (2). Data from the hybrid-E series are highlighted in red. DT shot N210808 is the datum in the upper-right of the plot, shown as the probability distribution from Markov chain Monte Carlo (MCMC) analysis with a contour enclosing 80% of the distribution.

form of a GLC and is not limited to 1D implosions, but more generally applies to any 3D configuration (with asymmetric modes <6),

$$ \text{GLC}_H = \bar{P}_{\text{HS}} \tau_{BW} H(T_{\text{HS}}) > 1, \quad (3) $$

where $H(T_{\text{HS}})$ is a complicated function of temperature [see Appendix C and Eqs. (27) and (28) of Ref. [107] and depends upon the measure of x-ray loss enhancement due to the potential presence of high-$Z$ mixing into the hot DT plasma, expressed by the $f_B \sim \bar{Z}^2 > 1$ of Eq. (1), with $\bar{Z}$ being the mass average atomic number. While not originally intended to correspond to a particular $Y_{\text{amp}}$ simulations show that GLC$_H = 1$ corresponds to a tight range of $Y_{\text{amp}} \sim 16–32$ for a wide range of DT implosion types [111], consistent with the prior metrics.

Figure 4 shows a plot of Eq. (3) with DT shot data. While Eq. (3) shows an uncertainty in the location of the ignition boundary, due to different high-$Z$ mix assumptions, the datum for experiment N210808 is above the range of ignition boundary uncertainty. This figure shows that the conclusion of N210808 passing the ignition boundary is insensitive to uncertainties in how much material has mixed into the hot spot.

Assuming that all α energy, $E_\alpha = Y/5$, remains in the DT hot spot, either by stopping in the hot spot directly causing heating (the $f_B$ stopping fraction) or by ablating the cold fuel surrounding the hot spot (1 − $f_B$) adding mass to the hot spot such that $d(mT_{\text{th}})/dt = 0$, an assumption that can be broken if $\alpha$’s are lost to pockets of cold plasma.
or exit the implosion via aneurisms], the parameter $E_a/(2E_{HS})$, where $E_{HS} = c_{DT} m T_{th} = (3/2) \rho_{HS} V$ is the hot spot internal energy, provides another ignition metric [113]. Namely, by comparison to a large suite of ICF simulations and from a semianalytic compressible shell model of the hot spot propagating into the surrounding shell, the transition to ignition has been found by Christopherson et al. [113]

$$\frac{E_a}{2E_{HS}} > 1.4, \quad \text{(4)}$$

where the factor of 2 in the denominator approximately accounts for the fact that only half the full yield of the implosion is generated at the time of peak burn. [Note that in Ref. [113], Eq. (4) is defined as "$f_a$" but that definition is not used here to avoid confusion with the $\alpha$ stopping fraction in Eq. (1).] The left frame of Fig. 5 plots Eq. (4) for the suite of NIF DT shot data with N210808 being the probability distributions to the upper right, again indicating ignition by a margin outside of the error bar of the inferred metric. Here, $E_{HS}$ is sensitive to the inference methodology; values from both 0D and 1D hot spot models [94] are shown (closed and open symbols as well as red and purple distributions, respectively).

Next, the ignition threshold experiment metric (ITFX) gives another alternative for assessing ignition. In simulations, the product of fusion yield in the 13–15 MeV energy range ($Y_{13−15}$) and the square of down-scatter ratio, DSR (the ratio of yield in the 10–12 MeV range over $Y_{13−15}$), correlate with $\gamma_{amp}$ and ignition as found by Spears et al. [30]. The most up to date version of ITFX is documented by Patel et al. [40]

$$ITFX_{no-\alpha} = ITFX_{\alpha} e^{-0.09 ITFX_{\alpha}^{0.47} + 0.007 ITFX_{\alpha}^{0.65}}, \quad \text{(5)}$$

where

$$ITFX_{\alpha} = \left( \frac{170 \, \mu g}{m_{\text{fuel}}} \right) \left( \frac{Y_{13−15}}{4.0 \times 10^{15}} \right) \left( \frac{\text{DSR}}{0.067} \right)^{2.1}, \quad \text{(6)}$$

where $m_{\text{fuel}}$ is the total DT fuel mass in the implosion. Equations (5) and (6) were obtained by fitting to a large database of simulations [114]. By construction, there is a 1:1 relationship between $ITFX_{\text{no-}\alpha}$ and $\gamma_{\text{amp}}$, namely $\gamma_{\text{amp}} = \exp(0.9 ITFX_{\alpha}^{0.47})$ (as reflected in right frame of Fig. 5). ITFX also has a simple approximate connection to the $\chi_{\text{no-}\alpha}$ Lawson-like ignition metric [101, 103, 110], namely, $\chi_{\text{no-}\alpha} \approx ITFX_{\text{no-}\alpha}^{0.34}$, making the two metrics interchangeable. As can be seen on the right frame of Fig. 5, experiment N210808 (the datum farthest to the right), passes the ITFX threshold for ignition, with a likelihood of 100%.

Several ignition criteria have been developed for the conditions reached in a space of areal density ($\rho R$) and temperature. Atzeni and Meyer-Ter-Vehn [108], Tipton [115] (most conservative case of the criteria by setting the cold fuel density term to zero), and Cheng et al. [116] have defined such criteria in terms of the hot spot areal density ($\rho R_{HS}$), while Coutant [117] considered total fuel
We have now considered several ignition metrics, which are summarized in Table II in terms of the likelihood of shots passing the criteria. We find that N210808 passes all criteria with high likelihood, except for the $G_{\text{target}} > 1$ definition of the 1997 NAS committee [109], which is not related to the physics of $\alpha$ heating, unlike the other criterion considered in this Letter.

While experiments with $G_{\text{fuel}} > 1$ have previously been reported [57,68], N210808 is the first ICF experiment to demonstrate capsule gain ($G_{\text{cap}} > 1$) achieving $G_{\text{cap}} \sim 5.8$. The overall target gain is $G_{\text{target}} \sim 0.72$, which is substantially larger than any prior ICF experiment, the highest of which (N210207) was $<0.09$ (Ref. [3], see Table I). That relatively modest changes were made to burning plasma experiments [3,4] to obtain the results in experiment N210808 emphasizes the sensitivity of ICF implosions near the ignition threshold. The fact that the DT plasma properties themselves jumped to significantly higher values, as reflected in the large change of $\rho_{\text{HS}}, T_{\text{th}}, V, E_{\text{HS}}, Y_{\text{total}},$ and $G$’s, is in itself a qualitative indication of ignition.

Efficient fusion fuel burnup requires the fusion rate per unit mass $Q_{\alpha} \sim T_{\text{th}}^2$ be as large as possible over the confinement time. Here, $n$ is well approximated by $7/T_{\text{th}}^{0.2}$, a decreasing function of $T_{\text{th}}$ (in kilo-electron-volts), with a local power law exponent sensitivity $7(1 - 0.2 \ln(T_{\text{th}}))/T_{\text{th}}^{0.2} = 3.4$ (2.4) for a 5 (10) keV Maxwellian distribution [119]. The gain of the system is ultimately limited by the fraction of fuel that can be “burned,” during a confinement time set by hydrodynamic expansion ($\sim R_{\text{HS}}/v$ where the expansion speed $v \sim \sqrt{T_{\text{th}}}$) which scales as the measurable product $\rho R T_{\text{th}}^{-0.5}$ [106]. Previous implosions have been limited to $<0.3\%$ burnup fraction [3] whereas this work reached 1.9%. Even the most maximally efficient ICF burnup fractions are realistically limited to levels of a couple $\sim 10^3 \%$, because the regime of strong propagating burn is truncated by explosion, rather than hot spot conduction and radiation losses.

In summary, the August 8, 2021 experiment on the National Ignition Facility is the first time that Lawson’s ignition criterion was unambiguously achieved in the laboratory. This demonstrates that the ignition threshold is real, largely consistent with theoretical expectations, and that a laboratory or reactor-scale plasma can be ignited. However, the demonstrated level of target gain on N210808, and the underlying scheme of x-ray driven implosions is not yet practical for fusion energy applications. Near repeat implosions since N210808 have reached 1/3 to 1/2 of the 1.3 MJ yield and corresponding lower $T_{\text{gas}}$, consistent with not having yet reached the expected performance plateau (i.e., not yet having “margin”) at the current areal density [106]. Attaining more robust and eventually higher yields have motivated plans to increase the areal density by scale and/or ablator-fuel thickness while maintaining similar $v_{\text{imp}}$ and coast time. This in turn will require further improving the hohlraum efficiency.

FIG. 6. NIF DT shot data (symbols) is plotted in the space of fuel areal-density [$\rho R$, hot spot only (top) and total (bottom)] and hot spot thermal temperature. The curves denote the ignition boundaries published in Cheng et al. [116], Tipton [115], Atzeni and Meyer-ter-Vehn [108], and Coutant [117].

areal density ($\rho_{\text{tot}}$). These criteria are shown in Fig. 6. In terms of hot spot areal density, several burning-plasma shots (Ref. [3]) are close to the boundary while N210808 clearly exceeds all these criteria. In terms of the $\rho_{\text{tot}}$ criterion from Coutant et al. [117], only N210808 passes the criterion. (Note some of these conditions neglect the mechanical energy loss of negative $pdV$ work and are thus unable to distinguish between a burning plasma and ignition.) Last, a criterion on the second derivative of temperature ($d^2T/dt^2 > 0$) at hot spot minimum volume, which represents that the implosion is thermodynamically prepared to heat even as the hot spot expands, was suggested by Rosen and Szoke [118] then later discussed in Springer [104]; N210808 is the first shot to pass as inferred from postshot simulations by Kritcher et al. [16].
(e.g., smaller LEHs, interior LEH shields [120,121], lower surface area to volume frustum-shaped “Frustraum” hohlraums [122]) and/or increasing NIF energy [123]. Further research tracks are aimed at improving compression of HDC and hence maximum attainable density and yield [124] by modifying laser pulse and dopant profile [125], using thicker ablators, revisiting high compression CH or other amorphous ablator designs in low gas-fill hohlraums with symmetry control by beam staggering [126] and adding magnetically assisted confinement [127]. Additionally, future studies will assess the impact of potentially non-Maxwellian distributions of D and T ions inferred from nuclear time-of-flight spectra [128].

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increasing DT fuel entropy and reducing compression. They were also impacted by hydrodynamic transfer (CBET) to the inner cone by three-wave mixing between beam cones to promote cross beam energy capability [152] during first shock passage [153], but also duration of the laser-pulse before the rise to peak power, see hohlraum radiation temperature, in the stronger first shock by raising the laser power, thus increasing compression [151].

Appendix A: History of ICF experiments on the NIF.— After developing on or adapting ICF instrumentation [129] and techniques [13] to the NIF to measure, and by adjusting laser and target parameters, control the peak drive [130,131], drive temporal profile [14,132], capsule trajectory [74], and symmetry [133–135], the 192 beam layered implosions began with intentionally dudded THD (tritium-hydrogen-deuterium) implosions [136,137]. The NIF commenced layered DT experiments in June 2011 with the “low-foot” design [15] that used a four-shock drive in a high gas fill (i.e., 0.96 mg/cm³ He) hohlraum to create a low entropy, hence high 30–35x convergence ratio (initial radius–stagnation radius), implosion using nominally 0.93 mm inner radius mid-Z doped CH polymer capsule ablators [138]. The hohlraum gas fill density was chosen to impede the hohlraum wall plasma expansion and maintain drive symmetry over the time duration required for the 20 ns low entropy pulse shapes. The 2011–2012 experiments [139,140] that reached 2.5 kJ yield were impacted by significant time-dependent laser-plasma instability (LPI) losses primarily on the inner cone [141] leading to undesirable implosion asymmetry swings [29,142–144] exacerbated by having to use fixed wavelength detuning between beam cones to promote cross beam energy transfer (CBET) to the inner cone by three-wave mixing [145]. They were also impacted by hydrodynamic instabilities [146–148] more than expected, as later proven by a brief “adiabat-shaping” series that raised the picket energy (first ∼1 ns) of the pulse [149] to reduce the ablation front instability [150] leading to a ∼3x increase in yield while maintaining relatively high compression [151].

A three-shock “high-foot” design [28,55] applies a stronger first shock by raising the laser power, thus hohlraum radiation temperature, in the “foot” (the time duration of the laser-pulse before the rise to peak power, see Fig. 1(b). The modification improves hydrodynamic stability [152] during first shock passage [153], but also increasing DT fuel entropy and reducing compression. The three-shock high foot accessed higher $T_{\text{ion}}$ and higher fusion yield [56] ultimately reaching 25 kJ [154], but asymmetry and the reemergence of instability capped performance as $v_{\text{imp}} \sim 390$ km/s was approached [155,156]. High-foot designs used the same targets as the low-foot design but with a higher (1.6 mg/cm³) helium gas fill, consequently it suffered from similar hohlraum problems (high LPI and poor symmetry control). During the high-foot series of experiments, it was first seen that reducing peak laser power while extending the duration of peak laser power, thus reducing coast time [herein quantitatively defined as mid-fall of the laser power at the end of the pulse to time of peak compression, see Fig. 1(b)], led to a significant simultaneous increase in implosion compression and fusion yield [157] and thus to the first indications of α-particle self-heating [57,158], albeit the physics behind the increase was speculative at the time.

Parallel efforts exploring so-called “exploding pushers” for neutron diagnostic flat-fielding [59,159] and traditional ablative designs [58,160] in near vacuum hohlraums mitigated losses due to LPI leading to a transition away from high gas-fill to low gas-fill hohlraums [161–163]. However, without a high gas fill, the ratio of hohlraum to capsule diameter needed to be larger for long pulse CH designs [164] to delay the ingress of hohlraum plasma into the path of the inner laser beams [165], reducing coupling efficiency from hohlraum to capsule. An alternate strategy reduced the pulse length by equalizing the picket and trough power at the expense of greater classical ablation front growth, applicable to Be ablator designs that compensate by more ablative stabilization of that growth [166].

To mitigate the lower energy coupling and poor symmetry control of CH ablators in high gas fill hohlraums, implosions using high density carbon (HDC) ablators were investigated. HDC ablators [167] doped with W for x-ray preheat shielding [168], which are relatively thinner than CH (for fixed capsule mass because of the density difference of 3.3–3.5 g/cm³ for HDC vs 1.05 g/cm³ for CH and 1.85 g/cm³ for Be), allowed for shorter laser pulses [169,170] and hence lower hohlraum He gas-fill (0.3 mg/cm³) while maintaining acceptable hohlraum wall ingress [66]. With lower gas pressures and shorter pulses, the energy lost to backscattered light was significantly reduced, increasing the overall coupling efficiency from 80% to 98%. Additionally, symmetry could be controlled without the need for CBET. Two-shock “BigFoot” [171–173] and three-shock “HDC” designs [174,175] of implosion were inherently even higher entropy and lower convergence due to the requirement to melt the crystalline HDC with a sufficiently strong first shock passage to avoid seeding instability growth at the ablator-fuel interface [169,176,177]. Such implosions reached 55 kJ of yield for similar capsule inside radius as earlier CH designs and seemed to be less affected by the hydrodynamic perturbations from the tent membrane (typically a 45 nm thick Formvar film that holds the capsule in the center of the hohlraum, see Fig. 1(a)] as predicted by high resolution capsule simulations [178], but were more susceptible to
hydrodynamic perturbations from the fill tube and hohlraum. Analysis of the experiments [51,179] and simulations [180] motivated an engineering effort to reduce the fill tube diameter. Three dimensional (3D) simulations performed with HYDRA suggest that megajoule yields could not be obtained [181] even if all degradations were removed from this initial HDC design. Theory and simulations indicated greater performance could be obtained with a larger capsule that absorbed more energy.

In parallel, experimentally observed limits [60] on convergence levels with HDC based ablators along with theory scalings based upon existing implosion data [61] motivated an alternate “HYBRID” (high yield big radius implosion design) strategy using larger capsules [61–63] to increase energy coupled to the hot spot without sacrificing stagnation pressure. Thus, in the “HYBRID-B” design, the capsule radius was increased by up to 20%, but the shell areal density was only increased in by 10% in order to maintain high $v_{imp}$ [182]. While the design was developed to eventually use 2.05 MJ of laser energy, implosions using the 1.9 MJ laser input available showed the expected improvement in yield for a given $v_{imp}$ by increasing scale [182]. These implosions also showed bright x-ray emission features [41] which correlated with reduced yield and an increase in imperfections in manufacturing larger capsules (voids in the bulk and pits on the surface), defects that remain an engineering challenge even today. Meanwhile, numerical modeling combined with data-driven models [66] for hohlraum wall motion dynamics [183–185], and for CBET developed for low gas-filled hohlraums [67] improved drive symmetry understanding and control. This enabled shrinking the hohlraum size by 5% for ~10% gain in efficiency while maintaining adequate drive symmetry in the “HYBRID-E” [54] and spool shaped “I-Raum” [186] designs. Fusion output on HYBRID-E and I-Raum designs reached 170 kJ and entered the burning plasma regime [3,4,53,187].

Appendix B: Laser improvements.—Laser pulse shaping and master oscillator design changes were implemented earlier in 2020 and 2021 to improve power accuracy and balance of NIF’s 192 beams in the hohlraum, contributing to improved implosion control and symmetry. Better control of the piccket power accuracy and peak of the pulse was achieved by updating the NIF laser master oscillator room (MOR) with currently available fiber optic modulation and amplification technologies and reducing amplifier gain uncertainty in the NIF four-pass preamplifiers. The newly deployed MOR architecture demonstrated a 2–3x shot-to-shot stability improvements of the pulse train before shaping and a mitigation of the power droop at the peak of ignition pulses [188]. Shot-to-shot gain stability of the preamplifier module employing a 32 mm diameter flashlamp-pumped LHG-8 Nd:glass rod amplifier improved from 5% rms to better than 3% rms.

FIG. 7. The contour plot of $H$ shows the dependence upon $f_B$ and $T$. At fixed $T$, higher $f_B$ lowers $H$ essentially reflecting the fact that enhanced bremsstrahlung cooling makes the ignition temperature higher than it would be for pure DT and this makes ignition more difficult to achieve. If the implosion can be engineered to have a high enough optical depth to reabsorb bremsstrahlung x rays ($f_B < 1$), the ignition temperature is reduced.

Appendix C: Thermodynamic ignition condition $H$ function.—The function $H(T)$ in Eq. (3) is (see Fig. 7)

$$H(T) = \frac{\sqrt{\pi f(T)}}{\sqrt{\frac{2\gamma}{\gamma - 1} + \frac{\gamma}{\gamma - 1} \frac{q}{T} \frac{\partial q}{\partial T}}}$$

(C1)

where $\gamma = 5/3$ is the polytropic index and the function $F(T)$ is a measure of the competition between $\alpha$ heating and bremsstrahlung cooling evaluated at peak hot spot pressure.

$$F(T) = \frac{3}{2} \frac{Q_\alpha - f_B Q_B}{\rho(\gamma DT)^2}.$$  

(C2)

The parameter $f_B$ reflects the DT bremsstrahlung enhancement at peak hot spot pressure. Note that $F = 0$ at the ignition temperature $T_{ign} = 4.3 f_B^{0.3}$ in keV.

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