Focal Molography: Coherent Microscopic Detection of Biomolecular Interaction

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We introduce and theoretically investigate here a novel analytical method that we have called focal molography, in which molecular interactions are made visible through scattering of coherent light by a coherent pattern of molecules. The scattered light quantifies the presence of molecules at molecular interaction sites. It is separated from noncoherent background scatter by a combination of local dark-field illumination, interference enhancement, and spatial filtering. The latter is achieved by holographic focusing of the wave field generated by the coherently assembled molecules onto an Airy disk and by subtraction of the noncoherent irradiance in the focal plane outside the disk from the irradiance in the disk. This new microscopic method allows distinct detection of low-refractive-index contrast in the nanoenvironment of biomolecules from which information on the interaction of the coherently assembled molecules with molecules in a liquid or gaseous sample may be deduced. The noncoherent surroundings of the coherently assembled molecules consist of freely diffusing solvent and solute molecules. The surroundings, as well as changes in temperature, do not contribute to the coherent signal in the diffraction focus. Interference lithography or high-resolution-imaging lithography can be used to synthesize the coherent pattern of molecules on a monolithic substrate. The coherent pattern of molecules constitutes a synthetic phase hologram that creates a diffraction-limited light wave. We suggest the term “mologram” for the coherent assembly of functional nanostructures and the term “focal molography” for label-free or labeled analysis of molecular interactions through the measurement of the properties of light in the focus of the mologram. We derive analytical formulas that express the detection signal and the sensitivity of focal molography on the surface of a high-refractive-index thin-film optical waveguide in terms of known parameters. We discuss the implementation of a readout system for molograms on a thin-film optical waveguide by adapting a confocal laser-scanning microscope to a bifocal laser-scanning microscope.

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I. INTRODUCTION

Phase contrast in transmitted light, discovered by Frits Zernike in 1934, revolutionized the biomedical research of living—i.e., unstained—cells [1]. The observation of polarizable molecular structures under the microscope made it possible to investigate subcellular components and the interaction of biological macromolecules (e.g., chromosomes) in their natural biological surrounding medium without the use of stains or labels [2]. In phase contrast (PhC), “direct light” and “diffracted light” from the same phase object are brought to interference [1,2]. PhC converts a small spatial phase modulation in the microscopic object into a visible intensity modulation, and, in this way, formerly invisible biological structures appear in dark or light contrast to the surroundings.

Digital holographic microscopy (DHM) in transmission mode is dedicated to the quantitative noninvasive investigation of refractive-index contrast or optical path length in three-dimensional phase objects, such as living cells in culture [3,4]. The DHM instrument is basically a Mach-Zehnder interferometer. A microscope objective collects direct light and diffracted light from the specimen and forms the object wave, which interferes, in off-axis geometry, with a reference wave to produce hologram intensity [3]. DHM uses numerical processing of the complex wave front in the digitally recorded hologram to compute small changes of phase contrast or optical path length in the specimen [3,4].

PhC and DHM enable the analysis of phase information produced by transparent specimens in high-resolution light microscopy. PhC and DHM allow one to study molecular interactions that can be measured through the detection of changes in the polarizability of the molecules in living cells. The optical manifestation of molecular processes in subcellular structures can be detected without the need for...
stains or fluorescent labels. PhC and DHM do not allow the
detection of the extremely small changes in refractive-index
contrast that accompany the interactions of biomolecules in
a sparse pattern of separated molecules. Noninvasive
investigation of biological specimens strives for new ways
and means that allow one to probe the phase contrast in
transparent microscopic specimens and to examine minus-
cule changes in phase contrast induced by biomolecular
processes.

The small spatial phase modulation that accompanies the
recognition and binding of molecules to immobilized bio-
molecules in a thin layer on the surface of a chip can—in
principle—be measured either by direct light or by diffracted
light. It is commonly believed that diffractometric optical
methods for the label-free detection of biomolecular inter-
actions cannot do any better than at present; i.e., they have
reached their physical limit. We demonstrate here that this
presumption does not apply. To help clarify our argument, a
brief review of the current situation is first presented.

The advent of sensitive refractometric optical biosensors
in the early 1990s [5,6] enabled the interactions between
biomolecules to be studied in much greater detail. In the
last two decades, a wide range of transducer principles was
developed to enable the direct monitoring of noncovalent
biospecific interactions between unlabeled biomolecules in
real time [7]. Refractometric optical biosensors measure the
resonance shift or the phase shift of a surface wave (surface
plasmon or waveguide mode) [7,8]. Label-free biomolec-
ular interaction analysis with optical biosensors requires the
immobilization of one interaction partner (the “receptor,” in
the parlance of this paper) in a thin layer on the sensor
surface to which a complementary interaction partner
(the “ligand”) may bind. The layer forms a thin phase
object that spreads over lateral dimensions of L with
L ≫ λ, and λ is the vacuum wavelength of the optical
surface wave. The thickness \( t_m \) of the phase object on the
supporting surface is small (\( t_m < λ \)), possibly as small as
approximately \( λ \times 10^{-6} \) [8]. Values of \( t_m \) below approx-
imately 0.1 nm resemble the averaged thickness of a
submonolayer [8]. The surface wave propagating along
the thin phase object is subjected to a phase retardation that
quantifies the concentration of ligand molecules at the
binding sites of the immobilized receptor [9,10].

Refractometric optical biosensors are used for the
characterization of molecular interactions in terms of both
affinity and chemical kinetics as well as for the concen-
tration analysis of a ligand in a sample that is brought into
contact with the sensor surface [5,6,10]. Since its intro-
duction in 1993, surface plasmon resonance (SPR) evolved
to the gold standard for measuring the kinetics of bio-
molecular interactions, i.e., the rates of complex forma-
tion (\( k_d \)) and dissociation (\( k_d \)) [10–14]. In drug discovery,
extinctive gratings described in Refs. [22] and
[23] are coupled into and out of the waveguide by
diffraction gratings, the measurement of the surface mass
density on this sensor surface is purely refractometric.
Every change of the refractive index within the penetration
depth of the evanescent field is recorded by the bidiffrac-
tive gratings-coupler biosensor through the measurement of
changes in the relative phase between the two coherently
excited modes of the thin-film waveguide (TE and TM).
Comprehensive investigations of the advantages and the disadvantages of the miniaturization of assays based on surface capture are discussed in Refs. [26] and [27]. The fundamental sensitivity limits of biosensors based on surface capture are analyzed in Ref. [27].

A. Limit of detection of refractometric optical biosensors for label-free biomolecular interaction analysis

Because refractometric optical biosensors use direct light for detecting molecular interactions, all refractive-index changes in the thin layer on the sensor surface (caused by nonbiospecific binding of ligand molecules to the sensor surface or to matrix molecules in the thin layer on the sensor surface, by changes of composition or ionic strength of the supernatant, or by small changes in temperature) contribute to the detected phase signal that is used for the deduction of the time-dependent course of the molecular interactions on the sensor surface.

The accumulated phase shift measured by refractometric optical biosensors (e.g., SPR and thin-film optical waveguide biosensors) depends on the propagation length of the waveguide. The propagation length is limited for SPR but not for waveguides. It is important to note that a given surface mass density results in a larger “specific phase shift” for SPR than for waveguides [9]. The specific phase shift is the phase shift per unit surface mass density and per unit propagation length of the surface wave. The phase shift that is induced by a given surface mass density (pg/mm²) divided by the propagation length of the surface wave is higher for SPR as compared to biosensors based on thin-film optical waveguides [9]. This is the reason why extensive research on label-free optical biosensors over the last 20 years has not changed the preeminent role of SPR in direct-binding assays [5,6,10–14]. The sensitivity of all refractometric optical biosensors in direct-binding assays is limited by small, unavoidable refractive-index changes that accumulate over the propagation path of the surface wave; it is not limited by the accuracy of the measurement of the total phase shift [8,9,11,12], which may be improved for waveguides by elongating the propagation path of the surface wave [8,9].

The hydrogel layer on the surface of the SPR biosensor consists mainly of water [16–18]. An increase in temperature of 0.02°C decreases the refractive index $n_0$ of the aqueous solution on the sensor surface by $\Delta n_0 \approx -2.2 \times 10^{-6}$. (The temperature dependence of the refractive index of water at $T = 25°C$ and $\lambda = 635$ nm is $dn/dT \approx -1.06 \times 10^{-4}1/°C$.) The hydrogel layer to which receptor molecules are immobilized is approximately 100 nm thick [18]. The association of approximately 1.2-pg/mm² protein with a 100-nm-thick layer on the sensor surface changes the refractive index $n_0$ of the layer by $\Delta n_0 \approx 2.2 \times 10^{-6}$ [15,18]. The phase shift induced by the binding of a small ligand to a relatively large immobilized receptor on the sensor surface is comparable to the phase shift caused by very small temperature instabilities during the measurement [11,14,18]. A minute instability in temperature during the measurement can readily override the phase shift measured by refractometric optical biosensors (SPR and thin-film optical waveguide sensors). This is the reason why refractometric optical biosensors need to utilize very precise temperature stabilization during the measurement of binding processes on the sensor surface.

Refractometric optical biosensors probe every change in refractive index in the thin layer on the sensor surface. Any change in composition of the freely diffusing solvent and solute molecules in the thin layer on the sensor surface caused by minute changes of composition or ionic strength of the supernatant contributes to the measured phase signal. This is the reason why highly sensitive label-free biomolecular interaction analysis with refractometric optical biosensors requires a steady flow of buffer solution with stable composition across the sensor surface during the measurement [5,6,10–14].

Nonbiospecific interactions of buffer constituents with the thin layer on the sensor surface can be compensated in the refractometric measurement by referencing the measured phase signal against a thin layer without receptor molecules [11,12,14]. Using this referencing-scheme quantification of pg amounts of ligand molecules per mm² in the thin layer on the sensor surface is possible with highly sensitive refractometric optical biosensors based on SPR [11,12,14].

B. Limit of detection of diffractometric optical biosensors for label-free biomolecular interaction analysis

In a recent paper [21], Nolte and co-workers argue that diffraction-based biosensors have a very low sensitivity to detection of the averaged thickness $d$ of small molecules or to thin layers of even larger molecules on the surface of the sensor chip because of the small value of $(d/\lambda)^2$ [21]. The new diffraction-based biosensor method described in this paper is able to overcome this deficiency of diffraction-based biosensors for label-free biomolecular interaction analysis by probing the diffracted wave in a diffraction-limited focal spot.

Focal molography provides signal amplification through the coherent addition of the phase signals from the coherently assembled molecules in the mologram by focusing of the phase signal from the coherently ordered molecules into a diffraction-limited focal spot. Focal molography has no apparent intrinsic lower limit of detection in terms of low receptor occupancy. It is shown below that the detection sensitivity of focal molography scales with the square of the diameter of the mologram. It is also shown that the sensitivity of focal molography is not limited by the unavoidable nonbiospecific interactions of solvent and solute molecules with the sensor surface or with matrix molecules in the thin layer on the sensor.
surface. Focal molography is expected to greatly increase the sensitivity and the detection accuracy of real-time label-free biomolecular interaction analysis.

II. FOCAL MOLOGRAPHY

This paper provides the theoretical basis for a new sensing concept, i.e., “focal molography.” The new concept has two unique advantages over existing label-free and labeled optical sensing methods: (i) It eliminates the effect of nonspecific binding that is the limiting factor in all current state-of-the-art sensing devices and (ii) it has a very high sensitivity that can theoretically be improved nearly without limitation by increasing the size of the sensor. Thanks to these properties, focal molography is expected to open new investigative possibilities in the analysis of affinity binding with high application potential in molecular biology and diagnostics.

A. Physical perceptions of focal molography

A value for the molecular scattering of light, in the analysis of Lord Rayleigh, may be obtained by summing the scattering from individual molecules (dipole scatterers). This calculation gives the same result as a calculation of the scattering from density fluctuations in the scattering medium. We consider now the scattering of coherent light by an isolated receptor-ligand complex. The intensity of near-backward scattering $I_{\text{scat}}$ by an isolated receptor molecule with refractive index $n_R$ embedded in a medium with refractive index $n_0$ in plane-polarized light is

$$
\frac{I_{\text{scat}}(r)}{I_R} = \frac{9\pi^2n_0^4}{r^2\lambda^4} \left( \frac{n_R^2 - n_0^2}{n_R^2 + 2n_0^2} \right)^2 V_R^2
$$

$$
= \frac{9\pi^2n_0^4}{r^2\lambda^4} \left( \frac{dn}{dc} \right)^2 \frac{M_R^2}{N_A} \hat{n}(\rho_R),
$$

(1)

where $r$ is the distance from the molecule to the point of observation, which is large compared to the vacuum wavelength $\lambda$ [28]. $I_R$ is the intensity of the plane-polarized field incident on the receptor molecule. The volume of the receptor molecule $V_R$ and the index factor $\hat{n}(\rho_R)$ are given by

$$
V_R = \frac{dn}{dc} \frac{M_R}{N_A(n_R - n_0)}; \quad \hat{n}(\rho_R) = \frac{(n_R + n_0)^2}{(n_R^2 + 2n_0^2)},
$$

(2)

where $M_R$ denotes the molar mass of the receptor molecule and $N_A$ the Avogadro constant. For the refractive-index increment $dn/dc$, we use the common value for proteins in water 0.182 ml/g [15,29,30]; this value is also a fairly good approximation for any biological ligand that may bind to the receptor in water $n_0 = 1.33$. The refractive index of a protein molecule depends on its mass density $\rho_R$: $n_R = n_0 + (dn/dc)\rho_R$. The index factor $\hat{n}(\rho_R)$ varies only slightly for different mass densities of the receptor protein in an aqueous medium: The three values of $\rho_R = 0.6, 1, 1.35$ g/ml result in values of $\hat{n}(\rho_R) = 0.244, 0.238, 0.233$, respectively. Thus, the mass of the receptor-ligand complex provides a generally applicable measure for the approximate calculation of the increase in the scattering intensity caused by the binding of a ligand molecule to the receptor molecule. The increase in scattering intensity caused by the binding of a ligand to the receptor is—in the first-order approximation—proportional to the square of the molecular masses of the receptor-ligand complex.

In a thought experiment, we consider the coherent scattering by a collection of $N_R$ isolated (i.e., separated) protein molecules embedded in a homogeneous medium $n_0$. The molecules are assumed to be localized in a thin layer with thickness $t_n \ll \lambda$ that forms an ellipsoid of revolution that has two optically conjugated foci $F$ and $F'$; see Fig. 1. The distance from the first focus $F$ to the ellipsoid of revolution and back to the second focus $F'$ is $2r$.

The molecules in the thin layer are irradiated by a diverging laser beam originating from the focus located at $F$. The coherently scattered light in the near-backward direction is confined to a diffraction spot (Airy disk) centered at $F'$. For a random distribution of the molecules in the thin layer, the diameter $d_A$ of the Airy disk is given by Abbe’s formula $d_A = \lambda/(2n_0 \sin \alpha)$, where $\alpha$ is half the opening angle of the diverging laser beam. We relate the coherently scattered power $P_{\text{scat}}$ incident on the Airy disk at $F'$ to the power $P_R$ (Disk-$d_A$) incident on a second disk with diameter $d_A$ located on the ellipsoid of revolution

$$
\frac{P_{\text{scat}}(\text{Airy})}{P_R(\text{Disk-$d_A$})} = \left( \frac{d_A}{r} \right)^2 \frac{N_R^2 M_R^2}{N_A^2} \hat{n}(\rho_R).
$$

(3)

Equation (3) is valid for a collection of $N_R$ molecules that form a coherent scattering system. For a given mass of protein in the thin layer, the ratio in Eq. (3) increases with decreasing $r$ in the second power of $(1/r)$. For the values

![FIG. 1. Coherent scattering by separated biomolecules in an aqueous medium.](image)
B. Focal molography on a thin-film optical waveguide

After consideration of these basic physical principles, we introduce and analyze a new microscopic method for probing extremely low-refractive-index contrast in a laterally elongated phase object with a thickness $t_m < \lambda$; a conceivable realization of it is shown in Figs. 2 and 3.

The investigated molecules are preferentially immobilized along the lines of a phase grating that forms a diffractive lens with diameter $D$ on the surface of a thin-film waveguide. The coherent pattern of molecules is referred to as a mologram. A diverging laser beam is coupled to the TE mode of the waveguide by an input coupler (focal grating coupler) of diameter $D$. While propagating through the mologram, the guided mode partially decouples from the waveguide through diffraction at the molecules in the mologram and forms a converging beam. The input coupler (IC) and the mologram constitute an integrated 3D-2D-3D optics imaging system with two optically conjugated foci $F$ and $F'$. Resonant coupling of the laser beam to a thin-film waveguide of high refractive index enhances considerably
the local light intensity that impinges on the mologram on the waveguide surface. The enhancement factor depends on the diameter \( D \) of the IC, its coupling efficiency, and on the optical parameters of the waveguide \[32\]. We consider a waveguide of high refractive index (e.g., Ta\(_2\)O\(_5\), \( n_f = 2.117, \lambda = 635 \text{ nm} \)) with thickness \( t_f = 145 \text{ nm} \) on a glass substrate with refractive index \( n_s = 1.521 \) covered with an aqueous medium with refractive index \( n_0 = 1.33 \). The effective thickness of the waveguide for the TE mode \( t_{\text{eff}} = t_f + \Delta x_{f,0} + \Delta y_{f,0} \) is 329 nm with the penetration depth into the cover medium \( \Delta x_{f,0} = 82 \text{ nm} \). A conservative estimate for the coupling efficiency of the beam impinging on the IC is approximately 30%; this value corresponds to a lune-shaped IC with diameter \( D = 0.4 \text{ mm} \) and a canonic surface-relief grating at the boundary between the waveguide and the substrate with a modulation depth of approximately 12 nm \[32\]. The stated parameters yield an enhancement factor of approximately 100 for the light intensity impinging on the mologram. Coupling of the incident beam to the waveguide gives rise to local dark-field illumination of the mologram on the surface.

The curved grating lines of the IC and the mologram with focal length \( f \) are defined through the equation

\[
\pm (x_j - \xi) = \frac{\lambda N (j_0 + j) - \sqrt{n_s^2(N^2 - n_s^2)(y_j^2 + f^2) + (n_s \lambda^2)(j_0 + j)^2}}{N^2 - n_s^2}.
\]

where \( j \) is the index of the line \((x_j, y_j)\). The \( \pm \) sign in Eq. (4) goes with the plus sign for the mologram and with the minus sign for the IC. The distance between the foci \( F \) and \( F' \) is \( 2\xi \). \( N = 1.814 \) denotes the effective refractive index of the TE mode of the Ta\(_2\)O\(_5\) waveguide. \( j_0 \) denotes the number of wavelengths in the substrate that add up to the focal length \( f \); thus, \( f = j_0 \lambda/n_s \). The lune-shaped mologram with diameter \( D = 400 \mu\text{m} \) and focal length \( f = 500 \mu\text{m} \) comprises approximately 600 lines; see Fig. 3. The distance between adjacent lines at their crossings of the symmetry axis of the grating structure varies continuously from approximately 338 to 267 nm for values of \( j \) between 62 and 663. To avoid the resonant case (second-order Bragg reflection) in the propagation path of the waveguide mode, the grating is omitted in the \( U \)-shaped central area of the IC and the mologram, where the magnitude of the coupling angle would be close to zero \[32\].

In focal molography, “diffracted light” from coherently assembled biomolecules is brought to interference in a diffraction-limited focus. The mologram diffracts and focuses the phase contrast of the coherently assembled molecules into an Airy disk. The diameter \( d_\lambda \) of the Airy disk is given by Abbe’s formula \( d_\lambda = \lambda/(2N.A.) \), where N.A. = \((n_f D)/(2f)\) is the numerical aperture of the mologram. For simplicity, the N.A. of the mologram is defined in analogy to the N.A. of a microscope objective; it does not take into account the lacking half in the lune-shaped mologram. The properties of the light in the focus of the mologram are used for distinct detection of refractive-index contrast in the proximity of the coherently assembled biomolecules from which information on the interaction of the immobilized biomolecules with molecules in a liquid or gaseous sample is obtained. The noncoherent surroundings of the coherently assembled biomolecules consisting of freely diffusing solvent and solute molecules (e.g., ions, detergents, plasma proteins, enzymes, cofactors, chaperons, ligand molecules) as well as changes in temperature do not contribute to the coherent signal in the focus of the mologram.

**C. Light-induced synthesis of the coherent pattern of molecules on a monolithic substrate**

We briefly describe here one possible route for creating the coherent pattern of receptor molecules on the sensor surface; see Fig. 4 and the Supplemental Material \[33\].

Nanopatterning, e.g., interference lithography \[34\], or high-resolution-imaging lithography, can be used to create a coherent pattern of receptor molecules with submicron resolution, which is a synthetic phase hologram that generates a diffraction-limited light wave out of a coherent pattern of molecules. State-of-the-art photolithography is suited for obtaining both submicron resolution and spatial coherence over the diameter \( D \) of the mologram; both features are required for the site-directed immobilization of the receptor molecules in the mologram.

The synthesis of the molographic nanopattern is preferentially accomplished within a thin hydrogel layer. The hydrogel layer has three key properties. First, before the application of biolithography to the layer, the layer on the sensor surface must be monolithic and homogeneous, both in terms of its chemical and its optical properties. Second, the layer carries linker molecules with a terminal functional group for immobilization of the receptor. The terminal group on the linker is initially protected by a photolabile protecting group for light-induced immobilization of the receptor. Finally, the layer on the sensor surface has to be resistant to nonbispesific protein adsorption \[35–37\].

The hydrogel layer on the sensor surface may be coupled to the surface of the Ta\(_2\)O\(_5\) waveguide through an intermediate self-assembled monolayer (SAM) \[37\] on the tantalum-oxide surfaces \[38\]. The SAM on the Ta\(_2\)O\(_5\) waveguide may consist of alkyl phosphate with a suitable functional group at the terminal position of the alkyl
The phosphate heads of the self-assembled alkyl phosphate provide the binding structure of the SAM layer to \( \text{Ta}_2\text{O}_5 \) [38].

The structure of one local period of the mologram on the sensor surface is not drawn to scale in Fig. 4: The hydrogel layer carrying the linkers to which the receptor molecules are immobilized may be much thicker than the SAM on the waveguide. The immobilized receptor molecules may be embedded within the hydrogel. The lines of higher refractive index in the mologram are denoted as “ridges,” while the lines of lower refractive index between the ridges are denoted as “grooves.” The immobilized receptor molecules are distributed in the ridges of the mologram. The grooves between the ridges might consist of hydrogel (nonbackfilled mologram) or of backfilled grooves (backfilled mologram). Ligand molecules and other biological constituents of the aqueous sample medium can freely diffuse through the hydrogel on the sensor surface [16,17,36].

Sensitive photochemistry for the deprotection of functional groups on linker molecules by photolysis is readily available [39–43]. The linker in the hydrogel is connected at one end to the hydrogel, while the other terminal group on the linker is protected by a photolabile protecting group for light-induced immobilization of the receptor within the hydrogel. Straightforward strategies based on the use of a photocleavable protecting group offer great potential for the control of biological organization at micrometer and nanometer length scales [41]. Suitable linker chemistry and photochemistry with excellent resistance to nonbiospecific protein adsorption are readily available for the lithographic synthesis of molograms for diverse applications [41–43].

The key steps of a possible route for creating the coherent pattern of receptor molecules in a homogeneous hydrogel layer on the sensor surface are outlined and illustrated in the Supplemental Material [33].

In Fig. 4, the binding of a ligand to the receptor is shown in (a) for a nonbackfilled mologram and in (b) for a backfilled mologram. In a backfilled mologram, only ligand molecules that are bound to receptor molecules contribute to the light intensity in the focus of the mologram. Backfilling of the mologram leads to vanishing diffraction intensity in the focus of the ligand-free mologram. Ideal backfilling is achieved with a perfect mimetic of the receptor that can be obtained, for example, through a point mutation in the binding pocket of the investigated receptor protein.

We propose the term “activation lithography” for light-induced immobilization of the mologram in a homogeneous layer on a monolithic substrate. The word “activation” indicates that the lithographic process is used for the activation of immobilization sites on the sensor surface. Activation lithography is used to direct the immobilization of biomolecules into a mologram that may be embedded in a hydrogel. Activation lithography does not affect the optical properties of the layered structure on the sensor surface.

When working with thoroughly optimized “protein-resistant” surfaces, the nonbiospecific adsorption of proteins from serum samples can be as low as 20–50 pg/mm² [24,35]. In surface-capture assays, nonbiospecific protein adsorption to the surface of the sensor chip can easily reach 100 pg/mm² or more [36]. Because molecules that nonbiospecifically adsorb to the layer on the sensor surface are homogeneously distributed across the layer, the nonbiospecific adsorption of proteins and other molecules on the sensor surface does not contribute to the light intensity in the diffraction focus of the mologram.

D. Sensitivity of focal molography

on a thin-film optical waveguide

In the following, we derive analytical formulas that estimate the detection signal and the expected sensitivity of the focal molography scheme depicted in Fig. 3 in terms of known parameters. From the leakage of the TE mode induced by the refractive-index modulation in the mologram, we calculate the power \( P_{\text{diff}} \) diffracted in the
half-spaces above and below the surface, respectively. The leakage power tends to divide equally between the two half-spaces [32]. With the leakage parameter $A_{\text{molo}}$ for the TE mode for a canonic grating with alternating rectangular cells of lower (in the grooves) and higher (in the ridges) refractive index, we obtain the following for a small power leakage across the area of a nonbackfilled mologram [32]:

$$\frac{P_{\text{diff}}}{P_{\text{wg}}} = \frac{A_{\text{molo}} \pi D}{4} = \frac{(n_m^2 - N^2)(n_m^2 - n_0^2)^2}{N(n_f^2 - n_0^2)} \frac{\Lambda t_m^2 \pi D}{\lambda^3 t_{\text{eff}}}, \quad (5)$$

where $t_m$ is the height of the rectangular cells in the canonic mologram. We assume $t_m \leq \lambda/20$, so the parabolic region of $A_{\text{molo}}$ applies [32]. $P_{\text{wg}}$ is the power of the TE mode impinging on the mologram. In Eq. (5), the field distribution of the guided mode is taken as invariant with $y$ for $|y| < D/2$ and 0 for $|y| > D/2$. The higher refractive index $n_m$ in the ridges is given by $n_m = n_0 + (dn/dc) c_R$, where $c_R$ denotes the concentration of the receptor in the ridges. $\Lambda = \lambda/n_m$ is the wavelength in the ridges [32]. For low $c_R$, we have $\Lambda \approx \lambda/n_0$. Relation (5) can be expressed in the well-known differential sensitivity $\partial N/\partial n_0$ of the refractometric thin-film waveguide biosensor [44]

$$\frac{P_{\text{diff}}}{P_{\text{wg}}} = \frac{\partial N}{\partial n_0} \frac{(n_m^2 - n_0^2)^2}{n_0} \frac{\Lambda t_m^2 \pi D}{\lambda^3 \Delta z_{f,0}} \frac{\partial N}{\partial n_0} \frac{8\pi n_0 \Lambda D}{\lambda^3 \Delta z_{f,0}} \frac{(dn)}{dc} \Gamma_{\Delta}^2, \quad (6)$$

with $\frac{\partial N}{\partial n_0} = \frac{n_0 n_f^2 - N^2}{N n_f^2 - n_0^2} \frac{\partial \Delta z_{f,0}}{n_f^2 - n_0^2} t_{\text{eff}}$. \quad (7)

The diffracted power $P_{\text{diff}}$ goes with the square of the surface mass-density modulation $\Gamma_{\Delta} = (t_m c_R)/2$ in the mologram. The refractive-index modulation $(n_m^2 - n_0^2)$ in Eq. (5) arises from regular density fluctuations of the molecules in the mologram and is given by the formula

$$(n_m^2 - n_0^2) = \left(2n_0 + \frac{dn}{dc} c_R\right) \frac{dn}{dc} c_R \approx 2n_0 \frac{dn}{dc} c_R. \quad (8)$$

The approximations in Eqs. (6) and (8) are valid for small $c_R$. For the stated waveguide parameters, $\partial N/\partial n_0$ equals 0.080 for the TE mode. We compare the power density of diffracted light on the Airy disk $P_{\text{diff}}(\text{Airy})$ to the power density irradiated on the input coupler. We relate $P_{\text{diff}}(\text{Airy}) = P_{\text{diff}}$ from (6) to the power $P_{\text{wg}}(\text{Disk}-d_A)$ incident on a disk with diameter $d_A$ in close proximity to the plane of the mologram. The “Disk-$d_A$” is located above or below the input coupler outside the intense field in the waveguide (see Fig. 3)

$$\frac{P_{\text{diff}}(\text{Airy})}{P_{\text{wg}}(\text{Disk}-d_A)} \approx \frac{\partial N}{\partial n_0} \frac{8\pi n_0 \Lambda D^3}{\lambda^3 \Delta z_{f,0}} \frac{(dn)}{dc} \Gamma_{\Delta}^2. \quad (9)$$

The expression for $P_{\text{diff}}(\text{Airy})$ from Eq. (6) that was inserted on the right side of Eq. (9) was divided by 4 to account for the lacking half in the lune-shaped mologram. For $n_0 = 1.33$, $n_s = 1.521$, $\lambda = 635$ nm, $\Lambda \approx \lambda/n_0 = 477$ nm, $D = 0.4$ mm, $f = 0.5$ mm [N.A. = $(n_f)/2f] = 0.61$, $\Delta z_{f,0} = 82$ nm, $dn/dc = 0.182$ mil/g, coupling efficiency of input coupler $\eta = 0.3$, and $\partial N/\partial n_0 = 0.080$, we obtain from Eq. (9) for $P_{\text{diff}}(\text{Airy})/P_{\text{wg}}(\text{Disk}-d_A)$ the values of approximately $2.3 \times 10^{-3}$ for 1-pg protein and approximately 2300 for 1-ng protein in the mologram, respectively. The diffracted power $P_{\text{diff}}(\text{Airy})$ irradiated by the coherently assembled molecules in the mologram is concentrated in a focal spot $F$ with diameter $d_A = (\lambda f)/(n_f D) \approx 0.52 \mu$m. The ratio $P_{\text{diff}}(\text{Airy})/P_{\text{wg}}(\text{Disk}-d_A)$ in Eq. (9) reaches the value 1 for approximately 21-pg protein in the mologram with $D = 0.4$ mm. This very small amount of coherently assembled biological material irradiates power density on the Airy disk in the focus of the mologram that equals the power density of the beam impinging on the input coupler; see Fig. 3. For comparison: One closely packed monolayer of water molecules on the surface area of the mologram with $D = 0.4$ mm contains approximately 39-pg water [8].

The calculated values $P_{\text{diff}}(\text{Airy})/P_{\text{wg}}(\text{Disk}-d_A)$ obtained from Eq. (9) for the mologram on the waveguide are about 40 times larger than the values $P_{\text{scat}}(\text{Airy})/P_{\text{wg}}(\text{Disk}-d_A)$ obtained from Eq. (3) for the coherent scattering system on the ellipsoid of revolution in a homogeneous medium $n_0$ that contains the same amount of biological matter as the mologram on the waveguide; see Figs. 1 and 3. The results obtained from Eqs. (3) and (9) are consistent with the intensity enhancement of the light impinging on the mologram on the thin-film optical waveguide that is caused by resonant coupling of the incident beam to the waveguide. The consistency of the two results is given within the expected uncertainties stemming from the approximations used in the two calculations on the different but physically related optical configurations, i.e., the power scattered by the coherent scattering system in Sec. II A and the power diffracted by the mologram on the waveguide in Sec. II D.

The light propagating in the waveguide is subjected to diffraction by the coherently assembled molecules on the waveguide and to scattering by small deviations from the perfect straightness of the waveguide walls [45]. The Ta$_2$O$_5$ waveguide is assumed to be prepared by ion beam sputtering. It has a propagation loss of approximately 0.8 dB/cm for the TE mode when covered with an aqueous medium. We assume that the propagation loss in the waveguide is entirely due to scattering of the propagating mode and that the scattered light is evenly distributed over the solid angle $4\pi$ [45].

We restrict the detection of the irradiance incident on the Airy disk to the aperture of the mologram. The ratio
between the diffracted power \( P_{\text{diff}}(\text{Airy}) \) and the scattered power \( P_{\text{scat}}(\text{Airy}) \) incident on the Airy disk is given by

\[
\frac{P_{\text{diff}}(\text{Airy})}{P_{\text{scat}}(\text{Airy})} = \frac{A_{\text{molo}}2n^2D^2}{A_{\text{scat}}\lambda^2} = \left(\frac{\partial N}{\partial n_0} 2^2\Delta \lambda^2 \cdot \frac{\partial n}{\partial c} \right)^2 \Gamma_{\Delta^2}. \quad (10)
\]

For \( n_0 = 1.33, \ n_s = 1.521, \ \lambda = 635 \text{ nm}, \ \Lambda \approx \lambda/n_0 = 477 \text{ mm}, \ D = 0.4 \text{ mm}, \ \Delta z_{f,0} = 82 \text{ nm}, \ \text{leakage parameter} \ A_{\text{scat}} = 10^{-2} \text{mm}^{-1} (0.8 \text{ dB/cm propagation loss}), \ dn/\partial c = 0.182 \text{ ml/g}, \ \text{and} \ \partial N/\partial n_0 = 0.080, \ \text{we obtain for} \ P_{\text{diff}}(\text{Airy})/P_{\text{scat}}(\text{Airy}) \ \text{the values} \ 30 \text{ for 1-pg protein and} \ 3 \times 10^7 \text{ for 1-ng protein in the thin mologram, respectively. The ratio} \ P_{\text{diff}}(\text{Airy})/P_{\text{scat}}(\text{Airy}) \ \text{in Eq. (10)} \ \text{reaches the value} \ 1 \ \text{for approximately 180-fg protein in the mologram with} \ D = 0.4 \text{ mm}. \ \text{This minuscule amount of} \ \text{coherently assembled biological matter} \ \text{radiates power density on the Airy disk in the focal plane of the mologram that equals the power density of the noncoherent irradiance of scattered light impinging on the focal plane of the mologram.}

The smallest possible refractive-index contrast of the ligand-free mologram can be attained by backfilling of the grooves between the ridges with an unreceptive (e.g., point-mutated) mimetic receptor \( R \). The binding of ligand molecules to the receptor \( R \) in the ridges of the canonic mologram changes the surface mass-density modulation \( \Gamma_{\Delta} \) in Eqs. (9) and (10), according to

\[
\Gamma_{\Delta^2} = [\Gamma_{\Delta^+}(c_R) - \Gamma_{\Delta^-}(c_R)]^2 + [\Gamma_{\Delta^+}(c_L) - \Gamma_{\Delta^-}(c_L)]^2 + 2[\Gamma_{\Delta^+}(c_R) - \Gamma_{\Delta^+}(c_L)] \approx [\Gamma_{\Delta^+}(c_L)]^2. \quad (11)
\]

\( \Gamma_{\Delta^+} \ \text{and} \ \Gamma_{\Delta^-} \ \text{denote the contribution of the ridges and the contribution of the grooves to the surface mass-density modulation in the mologram, respectively.} \ c_R \ \text{denotes the concentration of the inactive (e.g., point-mutated) receptor} \ R \ \text{in the grooves.} \ c_L \ \text{denotes the concentration of the ligand} \ L \ \text{in the ridges. For a nonbackfilled mologram,} \ c_R = \Gamma_{\Delta^-} = 0. \ \text{The approximation in Eq. (11) applies for perfect backfilling. Formula (11) applies to partial and full receptor occupancy.}

The noncoherent irradiance generated by scattering of the propagating mode at small deviations of the waveguide from perfect straightness is evenly distributed in the focal plane of the mologram [45]. The Airy disk is embedded in this background. The measured noncoherent irradiance in the focal plane outside the Airy disk can be subtracted from the measured power density in the Airy disk. The resulting value can be used for the accurate quantification of a molecular recognition and binding interaction of the coherently assembled receptor in the mologram with a freely diffusing ligand.

The calculation of the result (10) assumes that the radiation loss caused by the broad power spectrum of the small irregularities of the waveguide is evenly distributed over the solid angle \( 4\pi \). Actually, the Fourier components responsible for forward and backward scattering contribute more to the total radiation loss of the propagating mode than Fourier components causing scattering in other directions [45]. The preferential loss behavior of forward and backward scattering is not taken into account in Eq. (10). Thus, the result in Eq. (10) underestimates the amount of coherent irradiance in the diffraction focus of the mologram in relation to the scattered irradiance in the focal plane of the mologram. The ratio of the power density \( P_{\text{diff}}(\text{Airy}) \) of the diffracted light in the focus of the mologram divided by the power density \( P_{\text{scat}}(\text{Airy}) \) resulting from scattering of the guided mode is somewhat higher than the value given in Eq. (10).

The mologram is sensed by the evanescent field of the guided mode extending from the waveguiding film into the aqueous cover medium. The results (6), (9), and (10) are valid for thin molograms \( \lambda_{m} \leq \lambda/20 \approx 32 \text{ nm}, \ \text{i.e., in the parabolic region of} \ A_{\text{molo}} \ \text{vs} \ \lambda_{m} \ \text{and also for very thin molograms} \ (\lambda_{m} < 1 \text{ Å}), \ \text{where} \ \lambda_{m} \ \text{resembles the averaged thickness of a submonolayer. The distribution of the ligand molecules perpendicular to the surface only slightly changes} \ P_{\text{diff}} \ \text{as long as the mologram is thin} \ (\lambda_{m} < \lambda/20). \ \text{For a given waveguide, the sensitivity of focal molography in terms of the lowest detectable surface mass-density modulation} \ \Gamma_{\Delta} \ \text{decreases for thicker molograms. For molograms with} \ \lambda_{m} > \Delta z_{f,0}, \ \text{the contribution from molecules situated beyond the penetration depth} \ \Delta z_{f,0} \ \text{of the evanescent field on the leakage parameter} \ A_{\text{molo}} \ \text{decreases rapidly.}

Expressions analogous to Eqs. (5), (6), (7), (9), and (10) can be derived for the fundamental TM mode of the considered waveguide and for the higher modes of thicker waveguides [32,44]. The influence of the waveguide parameters on the sensitivities of focal molography for the TE and TM modes of the waveguide can be derived from the analysis of the differential sensitivities \( \partial N/\partial n_0 \) of the refractometric thin-film waveguide biosensor given in Ref. [44].

For relatively thick molograms having a thickness in the range of the penetration depth of the evanescent field, the sensitivity of focal molography may be enhanced by using a reverse-symmetry thin-film waveguide with a relatively low refractive index [46].

### E. Readout of the mologram through a bifocal laser-scanning microscope

Readout of the mologram is achieved by a confocal laser-scanning microscope with some add-on components in its beam path for the directional separation of incoupling and outcoupling. The add-ons make the confocal bifocal: Two beam stops (BSs), complementary to each other, restrict
half of the cross sections of the incident and the detection beam; see Fig. 5.

The incident laser beam is coupled to the waveguide via the objective and the focal IC, located alongside each mologram. A scan of F in the x direction adjusts the incident beam to the highest input coupling; see Fig. 3. The light decoupled by the mologram travels back via the scanner—i.e., the beam motion is neutralized again—and then passes through the beam splitter and is focused onto the optical plane of the pinhole (PH). The PH is adjusted in the x direction to maximize the light intensity on the detector. The detector behind the pinhole measures the light intensity in the focus of the mologram. The focal plane of the objective is adjusted to the plane parallel to the waveguide that contains the two foci F and F’. Scanning of the two foci F and F’ in three dimensions is required to measure the light intensity in the focus of the mologram at its maximum in terms of both input and output coupling. Two dimensions of the scan come from the fast scanner in the microscope and the third from the slide of the pinhole. The motion of the PH to a position away from F’ (or scanning of F in the y direction) can be used to measure the intensity of the noncoherent background and to deduct it from the intensity in F’.

Present-day confocal laser-scanning microscopes achieve multisite high-speed imaging through high-speed scanning with acousto-optic deflectors [47], which can generate fast discontinuous scanning patterns [47]. The diffractive nature of the acousto-optic deflection complicates the descanning of the nonmonochromatic light emitted from the fluorescent samples investigated by normal confocal laser-scanning microscopes. In the conceived bifocal laser-scanning setup, however, descanning is not a problem because the readout of the mologram on the sensor chip is monochromatic. Thus, the descanning of the outcoupled beam from the mologram in the acousto-optic deflector is not hindered by the diffractive nature of the acousto-optic deflection.

Acousto-optic deflection permits fast scanning and descanning of the monochromatic laser beams coupled into and out of the mologram with no macroscopically moving parts. The combined object scanning and beam scanning under the bifocal laser-scanning microscope is expected to be well suited for the readout of high-density mologram arrays on chips with the typical size of a microscope slide.

III. CONCLUSIONS AND FUTURE DIRECTIONS

In summary, we have a promising new analytical method—focal molography—that is expected to enable gentle, sensitive, and robust label-free probing of biomolecular interactions in real time. Biomolecules may be immobilized in a distinct submicron pattern within a thin hydrogel layer on the surface of a chip. Molecules that interact with the biomolecules in the thin layer get ordered. The induced order is comprehensively detected through diffracted light; direct light is shielded off. Hence, molecular interactions can be made visible by the measurement of changes of the phase contrast in the nanoenvironment of the immobilized biomolecules. In contrast to the currently used refractometric optical biosensors (SPR and optical waveguide sensors), focal molography is not hampered by the noncoherent surroundings of the coherently assembled molecules consisting of freely diffusing solvent and solute molecules.

Focal molography may evolve into an enabling method for the discovery of yet unknown biomolecular interactions and for the identification of molecules that interfere with protein-protein interactions. The biospecificity of the method can be enhanced considerably through the correlated detection of multiple recognitions of the targeted molecule (the analyte) by different interaction partners immobilized in multiplexed or superimposed molograms on the same surface.

The immobilization of small- and medium-size molecules that bind or may bind to proteins (known drugs, bioactive small molecules, synthetic peptide structures, and bioactive natural products) in an array of molograms to a very thin layer of affinity resin on a chip represents a promising potential application of focal molography for target identification by affinity capture through chemical proteomics in the pharmaceutical sciences [48,49]. In this particular application of focal molography, the small-molecule ligand is immobilized to the thin layer on the chip and the affinity of a much larger receptor protein to the small ligand is investigated through molographic readout. The problem is that many high-abundance proteins bind nonbiospecifically to the bare resin [48]. At this time, it is impossible to measure accurately the binding affinity of a
small molecule to its target protein without knowing the identity of the target protein [48]. This deficiency holds especially true for low-abundance target proteins [48]. Because focal molography is insensitive to the nonbiospecific binding of high-abundance proteins in the investigated cell extract to the bare resin, the new method may enable “bottom-up pull-down assays with in situ readout of the binding kinetics” of proteins that are captured by small- and medium-size immobilized binders in arrays of molograms.

Biomedical diagnostics based on molecular recognition involves the detection of low concentrations of known analytes with relatively high molecular weight (e.g., a protein, a peptide, or an oligonucleotide). Such analytes—they are also termed large-molecule diagnostic biomarkers—can be simultaneously recognized and bound by two complementary binding partners that interact with the analyte via complementary binding sites on the analyte. The second binder complements the first and carries a label. The immobilized binder captures the targeted analyte. The complementary binder binds via a complementary binding site to the analyte and forms a sandwich complex on the sensor surface. The sandwich complex consists of the immobilized binder, the analyte, and the complementary binder carrying the label [50]. The presence of the label on the sensor surface indicates the formation of a sandwich complex on the surface that, in turn, is an indication of the presence of the analyte in the investigated sample [50]. For refractometric optical biosensors, the labeling of the complementary binder to the targeted analyte is preferentially achieved with a high-refractive-index label such as a gold nanoparticle [24].

The focal molography method described in this paper can—in principle—also be applied to sandwich assays with a refractive-index label that enhances the refractive-index change associated with the formation of the sandwich complex on the sensor surface. Because focal molography detects only the coherently assembled nanoparticles on the surface of the chip—i.e., those particles that became ordered through the formation of the sandwich complex consisting of the immobilized binder, the analyte, and the complementary binder carrying the gold nanoparticle—a nanoparticle focal molography assay can be “separation free,” i.e., not requiring a washing step for separation of the bound and the free complementary binders in the boundary layer on the sensor surface before detection of the sandwich complex.

Methods for identifying and exploiting biomolecular interactions rely on two experimental steps: identification of intermolecular interaction partners by a variety of methods and high-resolution structure analysis of the complex formed by the bound partner molecules. The second step is mainly achieved by the x-ray crystallography of highly ordered crystals prepared by crystallogenesis of the binding partners; see, e.g., Refs. [51,52]. Even though the crystalline state of biomolecules is hardly ever encountered in nature, it has proven to be pivotal for our understanding of the interplay between the structure and the function of biomolecules [51,52]. The investigation presented in this paper was inspired by a scientific question: Besides densely packed protein crystals, is there a more “open” but still regular (i.e., coherent) man-made assembly of molecules that could facilitate the elucidation of biomolecular interactions? An “open coherent assembly” in this context means that the assembly has space between the molecules that can be accessed by molecules in a free solution. One main point to be considered is the absence of steric hindrance within the mologram. The mologram is an open and coherent assembly of immobilized molecules; it avoids steric hindrance that occurs from overcrowding of the molecules in the coherent assembly.

Focal molography, precisely because it utilizes the power of coherent and diffractive methodology, is highly sensitive and robust. Changes of the bulk refractive index in the thin layer on the sensor surface are noncoherent and do not contribute to the measured focal signal. Focal molography provides intrinsic discrimination of uncontrolled background signals that are due to nonbiospecific interactions in the boundary layer containing the coherently assembled biomolecules.

The realization of focal molography and experimental results will be presented in subsequent publications.

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