

Stabilization of Highly Polar BiFeO₃-like Structure: A New Interface Design Route for Enhanced Ferroelectricity in Artificial Perovskite Superlattices

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(Received 13 July 2015; revised manuscript received 26 January 2016; published 14 March 2016; corrected 25 March 2016)

In ABO₃ perovskites, oxygen octahedron rotations are common structural distortions that can promote large ferroelectricity in BiFeO₃ with an *R3c* structure [1] but suppress ferroelectricity in CaTiO₃ with a *Pbnm* symmetry [2]. For many CaTiO₃-like perovskites, the BiFeO₃ structure is a metastable phase. Here, we report the stabilization of the highly polar BiFeO₃-like phase of CaTiO₃ in a BaTiO₃/CaTiO₃ superlattice grown on a SrTiO₃ substrate. The stabilization is realized by a reconstruction of oxygen octahedron rotations at the interface from the pattern of nonpolar bulk CaTiO₃ to a different pattern that is characteristic of a BiFeO₃ phase. The reconstruction is interpreted through a combination of amplitude-contrast sub-0.1-nm high-resolution transmission electron microscopy and first-principles theories of the structure, energetics, and polarization of the superlattice and its constituents. We further predict a number of new artificial ferroelectric materials demonstrating that nonpolar perovskites can be turned into ferroelectrics via this interface mechanism. Therefore, a large number of perovskites with the CaTiO₃ structure type, which include many magnetic representatives, are now good candidates as novel highly polar multiferroic materials [3].

DOI: [10.1103/PhysRevX.6.011027](https://doi.org/10.1103/PhysRevX.6.011027)

Subject Areas: Materials Science

I. INTRODUCTION

New mechanisms to generate ferroelectricity (FE) have recently been the subject of active research because of both fundamental interest and the technological importance of ferroelectrics and related materials [4]. Novel ferroelectrics have potentially higher performance for practical applications, as well as potential compatibility with other functional properties such as magnetism, yielding multiferroics and other multifunctional materials [3,5,6].

Artificially structured perovskite superlattices offer rich opportunities for novel ferroelectricity [7–11]. Nonbulk phases for the constituent layers can be stabilized by the mechanical and electrical boundary conditions characteristic of a superlattice [12,13], potentially turning constituents that are nonpolar in bulk form into ferroelectrics [14,15]. Competing low-energy metastable phases can be readily found in perovskites with low tolerance factors, promoting

oxygen-octahedron-rotation (OOR) instabilities along the Brillouin-zone-boundary $R(1/2, 1/2, 1/2)-M(1/2, 1/2, 0)$ line. The ground-state structure in such cases is generally the nonpolar orthorhombic *Pbnm* structure. As a typical example, the oxygen octahedron in a CaTiO₃ (CTO) can be described by its rotation around the [110] axis and an in-phase rotation around the [001] axis ($a^-a^-c^+$ in Glazer notation). Such a pattern of OOR favors antipolar behavior instead of FE [2]. On the other hand, OOR with a different pattern can also promote large FE. As one famous example, in BiFeO₃ (BFO) with an *R3c* structure, the oxygen octahedron can be characterized by a rotation around [110] and an out-of-phase rotation around [001], yielding a fairly large polarization along [111] ($a^-a^-a^-$ in Glazer notation). Compared to the widespread use of CTO-like materials, BFO-like perovskites are relatively rarely seen. As a result, the OOR is generally thought to suppress FE in perovskites.

However, for many perovskites, the BFO-like structure serves as a low-energy metastable phase [2]. Therefore, it would be beneficial if an artificial perovskite superlattice could stabilize this metastable phase for the entire constituent layers or in a region near the interface. To this end, a reliable design mechanism can be derived only from precisely determined atomic positions in experiments

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followed by theoretical interpretations based on first-principles calculations.

II. EXPERIMENTAL AND FIRST-PRINCIPLES RESULTS

Aberration-corrected high-resolution transmission electron microscopy (HRTEM) is a powerful method for accurate visualization of oxygen octahedron distortions [16,17]. Recently, it was shown that amplitude contrast imaging in HRTEM could be used to discriminate heavy and light element columns based on channeling contrast [18], allowing one to locate the exact interface and to visualize OOR angles in different atomic layers (see Ref. [19]). Figure 1(a) shows an experimental HRTEM image of a 4BaTiO₃(BTO)/4CTO superlattice film along the [110] direction of the SrTiO₃ (STO) substrate. This image was obtained by correcting both spherical and chromatic aberrations to achieve amplitude contrast imaging conditions ($C_s = 3 \mu\text{m}$, $C_c = 1 \mu\text{m}$). In this image, channeling contrast between Ca and Ba columns is clearly observed: Atomic columns of CaO and BaO appear as bright and dark dots, respectively; oxygen and Ti columns appear as bright dots. Because of the interdiffusion of Ba and Ca at the interface, the intensity at the A site varies depending on the ratio of Ca and Ba as discussed in detail

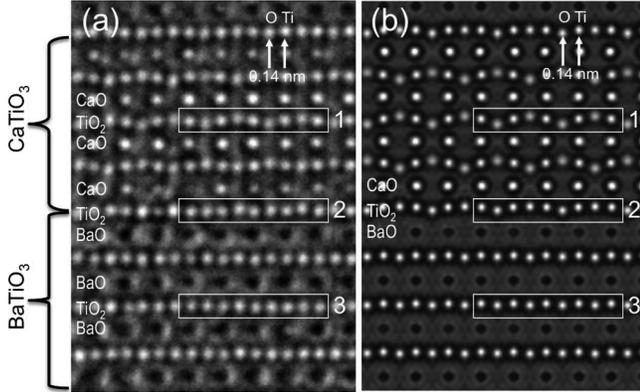


FIG. 1. Experimental and simulated HRTEM images showing oxygen octahedral tilts in the 4BTO/4CTO superlattice film grown on a STO substrate along [110]. (a) Experimental HRTEM image using an amplitude contrast imaging method ($C_s = 3 \mu\text{m}$, $C_c = 1 \mu\text{m}$, $\Delta f = -1 \text{ nm}$). BaO columns (dark dots) and CaO columns (bright dots) show different channeling contrast. Oxygen atomic columns displace differently, either upward or downward, with respect to the central Ti atoms in boxes 1, 2, and 3. Here, 0.14 nm indicates the spacing between Ti and O columns. The accumulated electron dose is $3 \times 10^4 \text{ electrons/nm}^2$. (b) Simulated HRTEM image using the atomic positions obtained from first-principles calculations. The simulated image matches well with the experimental image except for a sharper column contrast in the simulated image compared to the experimental one because electron-beam-induced object excitations are omitted, as pointed out by Kisielowski *et al.* (see Ref. [19]) [20].

in Ref. [19]. It is seen that BTO and CTO grow coherently on the STO substrate, showing the same in-plane lattice constant as that of STO, and an elongated c axis in the BTO layer and a shortened c axis in the CTO layer (see Ref. [19]). Within the CTO layer of the superlattice (box 1), a strongly corrugated TiO₂ plane is observed in which the oxygen atoms are displaced upward and downward with respect to the central Ti atoms, corresponding to an OOR around [110] by 9° , comparable to that of bulk CTO. For TiO₂ planes between two BaO planes (box 3), alternating displacement of the oxygen atoms, and thus the amplitude of the OOR, is negligible, consistent with the fact that bulk BTO strongly resists OORs. For TiO₂ planes between one BaO and one CaO plane (box 2), the OOR around [110] is 3° , smaller than that in the interior of the CTO layers.

For comparison, in Fig. 1(b), we present the simulated HRTEM image using the atomic positions of the 4BTO/4CTO superlattice obtained from first-principles calculations. The simulated HRTEM image for the computed structure shows the same pattern of OOR as in the experiment [compare boxes 1, 2, and 3 in Figs. 1(a) and 1(b)], with amplitudes of 12.5° in the CTO layer and 5.5° at the interface. The quantitative difference in OOR around [110] angles from the experimental observation can be partly attributed to the fact that the experiments were performed at $T = 300 \text{ K}$, while the ground-state structural relaxation by density functional theory was at $T = 0 \text{ K}$. In addition, in this image, it is possible to discern the small uniform displacement of the oxygen relative to the Ti atoms in the TiO₂ plane, which is associated with the spontaneous polarization of the superlattice. While this displacement is present in all the TiO₂ layers, it can be more easily identified in those belonging to the interior BTO layers, which do not have the corrugation associated with OOR.

We use the atomic-scale information from the first-principles results for a detailed layer-by-layer investigation of the properties of the superlattice. We focus our discussion on the 6BTO/6CTO superlattice, which allows a clearer distinction between the interface and interior layers; the corresponding results for the 4BTO/4CTO superlattice are similar (see Ref. [19]). The computed spontaneous polarization is $29 \mu\text{C cm}^{-2}$ along [001] and $11 \mu\text{C cm}^{-2}$ along [110]. The resulting layer-by-layer decomposed structural distortions and polarizations are shown in Fig. 2.

According to the dielectric slab model [14], the structure of the constituent layers of the superlattice should be closely related to those of strained bulk materials under the electrical boundary condition of a fixed displacement (D) field, imposed by the superlattice as summarized in Table I. Indeed, as shown in Fig. 2, the interior BTO layers have negligible OOR with a polarization of $32 \mu\text{C/cm}^2$ along the [001] direction. This is consistent with the structure and large polarization of strained BTO; the reduction from the strained bulk value of $42 \mu\text{C/cm}^2$ can be attributed to the electrostatic cost of polarizing

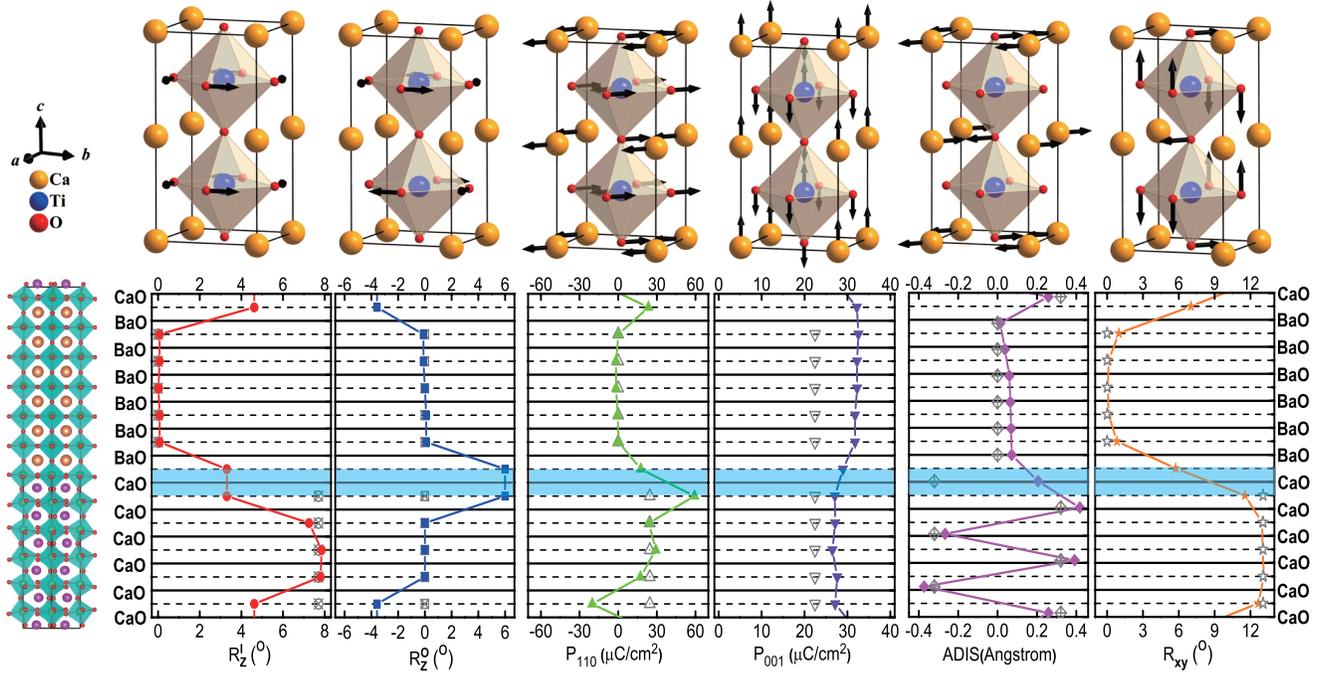


FIG. 2. Computed local properties associated with ferroelectric and nonpolar modes in 6BTO/6CTO superlattice and schematic plots for the atomic displacements of the oxygen octahedron rotation and ferroelectric modes. First-principles calculations of a 6BTO/6CTO superlattice showing layer-by-layer decompositions of in-phase oxygen octahedron rotation around [001] R_z^i , out-of-phase oxygen octahedron rotation around [001] R_z^o , in-plane polarization P_{110} , out-of-plane polarization P_{001} , antipolar modes (AFE) represented by A-site cation displacements (ADIS), and oxygen octahedron rotation around [110] R_{xy} . The corresponding strained bulk values are also denoted by the open symbol in the plot, and in particular, the open strained bulk values in P_{001} are predicted by the dielectric slab model [14]. A highly polar BiFeO₃-like interface phase in CTO is highlighted in blue.

the nonpolar CTO layer. Both bulk CTO and strained bulk CTO are characterized by the strong OORs due to structural instabilities at the zone-boundary M and R points. Therefore, the interior CTO layers are dominated by R_{xy} and R_z^i , which are OOR around [110] and an in-phase OOR around [001], respectively, as shown in Fig. 2. In addition, a large antipolar (AFE) mode develops in the CTO layers that can be clearly identified by the zigzag movement of A-site displacement along the [110] direction. It should be stressed that this antipolar distortion is a structural distortion at the X point favored by the trilinear coupling due to the pattern of OOR in CTO-like materials. The above distortion in the interior CTO layers can be clearly seen in Fig. 2, as well as in the TEM image in Fig. 1(a) (see Ref. [19]). This AFE mode was also recently pointed out to be the key to the suppressed FE in all CTO-like perovskites [2]. Because of the applied tensile epitaxial strain, the interior CTO layers are polar along the [110] direction with a magnitude of $26.4 \mu\text{C}/\text{cm}^2$ just like the strained CTO [21].

If the interface effect is negligible, the dielectric slab model can be used to predict the polarization, yielding a value of $22.4 \mu\text{C}/\text{cm}^2$ along the [001] direction. The first-principles calculation gives $P_{001} = 29.0 \mu\text{C}/\text{cm}^2$. The discrepancy from the dielectric slab model suggests that the interface effect cannot be neglected. Such a large

enhancement of the polarization (about 25%) is a strong indication of a highly polar interface reconstruction. Indeed, examination of Fig. 2 reveals that the structure

TABLE I. Computed bulk properties of $R_z^i(\circ)$, $R_z^o(\circ)$, $R_{xy}(\circ)$, ADIS (\AA), $P_{001}(\mu\text{C}/\text{cm}^2)$, $P_{110}(\mu\text{C}/\text{cm}^2)$, total polarization $P_T(\mu\text{C}/\text{cm}^2)$, c/a ratio, and the total energies (eV) for strained BTO and CTO on STO substrate modeled in 20-atom supercells. Both fixed electric (E) field and displacement (D) field boundary conditions are considered, which are used to describe the electric boundary conditions of a perovskite in its natural bulk or within an insulating superlattice.

Boundary Condition	Fixed E field $E = 0 \text{ V/m}$			Fixed D field $D = 29 \mu\text{C}/\text{cm}^2$	
	BaTiO ₃	CaTiO ₃	CaTiO ₃	CaTiO ₃	CaTiO ₃
Perovskite	BaTiO ₃	CaTiO ₃	CaTiO ₃	CaTiO ₃	CaTiO ₃
Symmetry	P4 mm	Pbnm	e-R3c	Pbnm	e-R3c
R_z^i	0	7.7	0	7.6	0
R_z^o	0	0	7.3	0	7.2
R_{xy}	0	12.7	11.5	12.8	11.7
ADIS	0	0.29	0	0.32	0
P_{001}	41.93	0	20.01	27.81	28.96
P_{110}	0	26.40	52.19	24.53	51.25
P_T	41.93	26.40	55.89	37.08	58.87
c/a	1.067	0.964	0.968	0.965	0.967
Energy	-162.645	-164.158	-164.066	-164.106	-164.040

at the interface of the CTO layers differs significantly from that of the strained bulk CTO, with the OOR being suppressed at the interface of the superlattice. The AFE-type displacement, which is driven by the trilinear coupling [2] involving the OORs of CTO, is suppressed too. Furthermore, a new structural pattern of OOR emerges at the interface: an OOR around the [110] axis and an out-of-phase OOR around the [001] axis for a TiO_6 sandwiched between two interface CaO layers, with rotation angles comparable to those of the strained bulk in-phase OOR. This new structure pattern is exactly the same as one would observe for oxygen octahedron rotation in BiFeO_3 and similar perovskites with $R3c$ symmetry.

III. MICROSCOPIC MECHANISM

Here, we propose that this change in structure at the interface can be interpreted as the local stabilization of a BFO-like structure different from that of the bulk CTO. As far as the topology of the oxygen octahedron rotation network is concerned, oxygen octahedra in both BFO and CTO rotate around [110]; however, BFO differentiates itself from CTO by its out-of-phase OOR around [001] instead of the in-phase counterpart in CTO. The out-of-phase and in-phase OORs around [001] originate from symmetry-nonequivalent structural instabilities at the R and M points, respectively. This stabilization of a BFO-like structure in CTO layers near the interface is derived from the metastable polar e - $R3c$ phase and is compatible with a much larger polarization than that in bulk CTO, as shown in Table I. It has been shown that this phase cannot be stabilized relative to the $Pbnm$ phase by epitaxial strain alone [22]. However, in the superlattice, the suppression of the tilt angles by proximity to BTO, assisted by the electrical and mechanical boundary conditions that favor a phase with a component of polarization along [001], is sufficient to stabilize the structure [23].

To explore the stabilization of this phase more quantitatively, we constructed first-principles-based models for the strained $Pbnm$ phase [designated $E_{\text{CTO}}(\mathbf{R}_z^i, \mathbf{R}_{xy}, \text{AFE}_{xy}, \text{FE}_{xy})$] and for the metastable e - $R3c$ phase [$E_{\text{BFO}}(\mathbf{R}_z^o, \mathbf{R}_{xy}, \text{FE}_{xy}, \text{FE}_z)$]. Facilitated by space-group-symmetry analysis, the models of both E_{CTO} and E_{BFO} are built through polynomial expansions of the total energy from first-principles calculations with respect to the high-symmetry reference structure ($P4/mmm$ phase) in terms of the amplitudes of the relevant modes. In the above, \mathbf{R}_z^i , \mathbf{R}_z^o , \mathbf{R}_{xy} , AFE_{xy} , FE_{xy} , and FE_z represent the mode amplitude of in-phase OOR around [001], out-of-phase OOR around [001], OOR around [110], the in-plane antipolar mode, and the in-plane and out-of-plane FE modes, respectively. The resulting models are shown in the following for E_{CTO} and E_{BFO} , respectively, as (see Ref. [19] for fitted coefficients)

$$\begin{aligned}
 E_{\text{CTO}} = & a_1 \mathbf{R}_z^i{}^2 + b_1 \mathbf{R}_z^i{}^4 + a_2 \mathbf{R}_{xy}^2 + b_2 \mathbf{R}_{xy}^4 + a_3 \text{AFE}_{xy}^2 \\
 & + b_3 \text{AFE}_{xy}^4 + a_4 \text{FE}_{xy}^2 + b_4 \text{FE}_{xy}^4 + c_1 \mathbf{R}_z^i{}^2 \mathbf{R}_{xy}^2 \\
 & + c_2 \mathbf{R}_z^i{}^2 \text{AFE}_{xy}^2 + c_3 \mathbf{R}_z^i{}^2 \text{FE}_{xy}^2 + c_4 \mathbf{R}_{xy}^2 \text{AFE}_{xy}^2 \\
 & + c_5 \mathbf{R}_{xy}^2 \text{FE}_{xy}^2 + c_6 \text{AFE}_{xy}^2 \text{FE}_{xy}^2 + d_1 \mathbf{R}_z^i \mathbf{R}_{xy} \text{AFE}_{xy},
 \end{aligned} \tag{1}$$

$$\begin{aligned}
 E_{\text{BFO}} = & \alpha_1 \mathbf{R}_z^o{}^2 + \beta_1 \mathbf{R}_z^o{}^4 + \alpha_2 \mathbf{R}_{xy}^2 + \beta_2 \mathbf{R}_{xy}^4 + \alpha_3 \text{FE}_z^2 \\
 & + \beta_3 \text{FE}_z^4 + \alpha_4 \text{FE}_{xy}^2 + \beta_4 \text{FE}_{xy}^4 + \gamma_1 \mathbf{R}_z^o{}^2 \mathbf{R}_{xy}^2 \\
 & + \gamma_2 \mathbf{R}_z^o{}^2 \text{FE}_z^2 + \gamma_3 \mathbf{R}_z^o{}^2 \text{FE}_{xy}^2 + \gamma_4 \mathbf{R}_{xy}^2 \text{FE}_z^2 \\
 & + \gamma_5 \mathbf{R}_{xy}^2 \text{FE}_{xy}^2 + \gamma_6 \text{FE}_z^2 \text{FE}_{xy}^2 + \kappa_1 \mathbf{R}_z^o \mathbf{R}_{xy} \text{FE}_z \text{FE}_{xy}.
 \end{aligned} \tag{2}$$

Assuming the angles of the oxygen octahedron rotations are tunable parameters under experimental conditions, we further define the functions $\mathcal{F}_{\text{CTO}}(\mathbf{R}_z^i, \mathbf{R}_{xy}) = \min_{\text{AFE}_{xy}, \text{FE}_{xy}} E_{\text{CTO}}(\mathbf{R}_z^i, \mathbf{R}_{xy}, \text{AFE}_{xy}, \text{FE}_{xy})$ and $\mathcal{F}_{\text{BFO}}(\mathbf{R}_z^o, \mathbf{R}_{xy}) = \min_{\text{FE}_{xy}, \text{FE}_z} E_{\text{BFO}}(\mathbf{R}_z^o, \mathbf{R}_{xy}, \text{FE}_{xy}, \text{FE}_z)$. In order to understand how the BFO-like phase can be stabilized relative to the CTO-like phase, we then evaluate $\Delta E = \mathcal{F}_{\text{BFO}} - \mathcal{F}_{\text{CTO}}$ as functions of oxygen-octahedron-rotation magnitudes around [110] and [001]. The resulting ΔE is presented in Fig. 3. The total FE mode amplitudes are also presented by the color spectrum in the base plane in Fig. 3. It can be seen that when the angles are fixed to the values of bulk CTO regions in the superlattice, as shown in

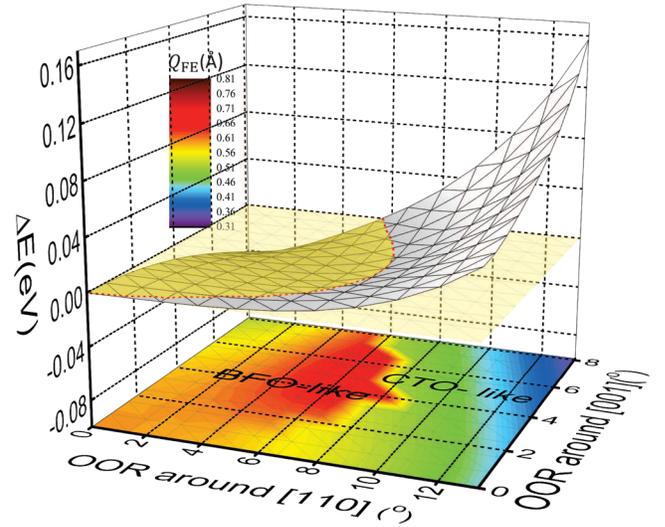


FIG. 3. Appearances of both BiFeO_3 -like and CaTiO_3 -like phases and the transition from one to the other as functions of oxygen octahedral rotations in strained bulk CaTiO_3 . We show phase stabilities studied by the relative energetics between the BFO-like and CTO-like phases as plotted by ΔE as functions of magnitudes of oxygen octahedral rotation around [001] and [110], respectively. The FE mode amplitudes are represented by projected colors in the base as well.

Fig. 2 ($R_z^i = 8.3^\circ$ and $R_{xy} = 12.6^\circ$), the CTO-like phase is strongly favored in energy. In the CTO-like phase, as shown in Fig. 2 and Table I, the antipolar distortion is favored over the FE distortion due to the large trilinear coupling term $\sim R_z^i R_{xy} A F E_{xy}$ in Eq. (1). Notably, when the amplitudes of the OORs are reduced, the BFO-like phase becomes energetically more stable than the CTO-like phase, as shown in Fig. 3. This indicates that the BFO-like phase can be stabilized over the CTO-like phase when the OOR is reduced. When the above transition takes place, the OOR around [001] will change abruptly from in-phase rotation to out-of-phase rotation, signifying a more drastic change in the topology of the oxygen octahedron network, as guided by the yellow plane at $\Delta E = 0$ in Fig. 3. In addition to the pattern change of OOR, the BFO-like phase is generally found to have much larger polarization than that in the CTO-like phase, as shown by the color spectrum in Fig. 3. The much stronger FE polarization is expected, originating from the *e-R3c* phase; it can also be easily understood by the large four-linear coupling term $\sim R_z^o R_{xy} F E_z F E_{xy}$, which promotes FE in both the in-plane and out-of-plane directions.

This mechanism leads to the BFO-like phase that exists at the interface of the BTO/CTO superlattice. Assuming the octahedra to be fairly rigid, the reduction of OOT is imposed by the adjoining BTO layer, which is strongly resistant to the OOR. A direct consequence of the stabilization of the BFO-like structure at the interface is that the polarization of the superlattice is greatly enhanced. For a particular choice of angles with $R_z^o = 5.7^\circ$ and $R_{xy} = 6.6^\circ$ similar to those at the interface of the BTO/CTO superlattice, the computed polarization of the BFO-like phase is over $54.0 \mu\text{C}/\text{cm}^2$, which is comparable to the polarization in the bulk *e-R3c* CTO as shown in Table I. In the superlattice, the BFO-like phase is further favored by both the electric and mechanical boundary conditions imposed by the polarization of the BTO layer according to Eq. (2). Under the continuous displacement field along the [001] direction, the electric boundary condition tends to polarize the CTO components with a larger $F E_z$. Under the tensile strain, the mechanical boundary condition effectively enhances $F E_{xy}$. The larger $F E_z$ and $F E_{xy}$ tend to further

lower the energy through $\sim R_z^o R_{xy} F E_z F E_{xy}$ and stabilize the BFO-like phase.

IV. INVERSE DESIGN OF NEW FERROELECTRIC MATERIALS

It has long been recognized that oxygen octahedron rotation can play different roles in perovskites promoting FE in BFO-like materials [1,24] but suppressing FE in CTO-like materials [25]. However, the results presented here suggest that a transition between these two phases can be achieved through interface engineering in a superlattice. In addition to improving the fundamental understanding of these transitions, these results suggest a new pathway to induce FE in functional oxide materials.

The enhanced polarization observed in the BTO/CTO superlattice studied here demonstrates this mechanism. To explore the potential of this approach, we predict a few more superlattices $A'B'O_3/A''BO_3$ as listed in Table II. Within this category of tailored materials, one of the parent bulk $A'B'O_3$ is chosen to be a CTO-like perovskite with strong oxygen octahedron rotations, resulting in an anti-polar-type (CaTiO_3 and CdTiO_3) [26] or an antiferroelectric-type (AgNbO_3 and NaNbO_3) [27,28] ground state that is favored by the trilinear coupling term. The other parent bulk $A''BO_3$ is chosen to have a large tolerance factor resisting oxygen octahedron rotation and a strong FE polarization. Similar to what we have already shown for the BTO/CTO example, the out-of-phase OORs around [001] are induced around the interface layers of $A'B'O_3$ (see Ref. [19] for examples of $2\text{BaTiO}_3/2\text{CaTiO}_3$ and $2\text{KNbO}_3/2\text{AgNbO}_3$). As a result, the overall polarizations of the superlattices are enhanced compared to the predictions from the dielectric slab model, which is equivalent to applying the charge continuity principle only and completely neglecting the possible interface reconstruction.

This approach to create new FE materials by interfacial control can also be used to create new materials even when the building blocks could come *only* from nonpolar perovskites. In Table III, we list a few predicted $1A'B'O_3/1A''BO_3$ superlattices within this category. These interface materials also provide a good opportunity to perform rigorous mode decompositions based on space

TABLE II. Predicted superlattices with enhanced polarizations. $P_{A'BO_3}^{\text{sbulk}}$ ($\mu\text{C}/\text{cm}^2$) and $P_{A''BO_3}^{\text{sbulk}}$ ($\mu\text{C}/\text{cm}^2$) denote the computed polarizations for strained $A'B'O_3$ and $A''BO_3$ respectively. P_M ($\mu\text{C}/\text{cm}^2$) and P_{Cal} ($\mu\text{C}/\text{cm}^2$) are the expected polarizations from the dielectric slab model [14] and the computed polarizations from first principles in $nA'B'O_3/nA''BO_3$, respectively. Polarization enhancement is calculated by $(P_{\text{Cal}} - P_M)/P_M$. The last column is the proposed substrate for the epitaxial growth of the superlattice.

$nA'B'O_3/nA''BO_3$	$P_{A'BO_3}^{\text{sbulk}}$	$P_{A''BO_3}^{\text{sbulk}}$	P_M	P_{Cal}	Enhanced	Substrate
$2\text{BaTiO}_3/2\text{CaTiO}_3$	41.9	25.7	25.5	39.9	56%	SrTiO_3
$2\text{BaTiO}_3/2\text{CdTiO}_3$	50.8	37.8	34.2	50.4	47%	NdGaO_3
$2\text{KNbO}_3/2\text{NaNbO}_3$	36.2	~ 0	19.8	37.5	89%	DyScO_3
$2\text{KNbO}_3/2\text{AgNbO}_3$	36.2	~ 0	22.0	38.2	73%	DyScO_3

TABLE III. Predicted new artificial ferroelectric materials based on nonpolar perovskites. The columns are as follows. (1) Mode decompositions (\AA) of $Q_{R_z^o}$ as out-of-phase OOR around [001], $Q_{R_z^i}$ as in-phase OOR around [001], $Q_{R_{xy}}$ as OOR around [110], Q_{FE_z} as polar distortion along [001], $Q_{FE_{xy}}$ as polar distortion along [110], and $Q_{AFE_{xy}}$ as in-plane antipolar distortion. Their symmetries are labeled as $M_1^-, M_3^+, M_5^-, \Gamma_3^-, \Gamma_5^-$, respectively. (2) OOR angles (degrees) R_z^o, R_z^i, R_{xy} for out-of-phase OOR around [001], in-phase OOR around [001], and OOR around [110] (octahedron tilt), respectively. (3) The polarizations ($\mu\text{c}/\text{cm}^2$) along the [001] direction P_{001} and along the [110] direction P_{110} , and the total polarization P_T . (4) The polarization enhancement. (5) Substrate for the epitaxial growth of the superlattices, KTaO_3 ($a = 3.99 \text{ \AA}$) and MgO ($a = 4.21 \text{ \AA}$). (6) Space group symmetry of both the strained bulk and superlattice.

$A'(A'')\text{BO}_3$ $nA'\text{BO}_3/nA''\text{BO}_3$	Mode decompositions (\AA)						OOOR angles ($^\circ$)			Polarization ($\mu\text{c}/\text{cm}^2$)			Enhancement	Substrate	Symmetry
	$Q_{R_z^o}$	$Q_{R_z^i}$	$Q_{R_{xy}}$	Q_{FE_z}	$Q_{FE_{xy}}$	$Q_{AFE_{xy}}$	R_z^o	R_z^i	R_{xy}	P_{001}	P_{110}	P_T			
CdSnO_3	0	1.22	1.85	0	0	0.79	0	12.0	17.7	0	0	0	...	KTaO_3	Pnma
BaSnO_3	0	0	0	0	0	0	0	0	0	0	0	0	...	KTaO_3	$P4/mmm$
$1\text{CdSnO}_3/1\text{BaSnO}_3$	1.08	0	1.21	0.20	0.60	0	9.4	0	12.2	8.9	13.5	16.2	∞	KTaO_3	Pc
CdHfO_3	0	1.27	1.74	0	0	0.69	0	12.3	16.9	0	0	0	...	KTaO_3	Pbnm
BaHfO_3	0	0	0	0	0	0	0	0	0	0	0	0	...	KTaO_3	$P4/mmm$
$1\text{CdHfO}_3/1\text{BaHfO}_3$	1.07	0	1.17	0.18	0.64	0	9.3	0	12.2	7.8	10.8	13.3	∞	KTaO_3	Pc
CaZrO_3	0	1.02	1.82	0	0	0.72	0	9.2	16.2	0	0	0	...	MgO	Pcmm
BaZrO_3	0	0	0	0	0	0	0	0	0	0	0	0	...	MgO	$P4/mmm$
$1\text{CaZrO}_3/1\text{BaZrO}_3$	0.79	0	1.22	0.27	0.71	0	6.6	0	10.8	11.1	27.6	29.7	∞	MgO	Pc
$1\text{CaZrO}_3/1\text{BaZrO}_3$	0.90	0	1.16	0.30	0.67	0	8.1	0	10.6	13.5	22.5	26.2	∞	Relaxed	Pc

group theory followed by a careful comparison between the interface materials and the parent bulk compounds. The resulting mode decompositions and the local properties are also shown in Table III. The $A'\text{BO}_3$ is again a CTO-like perovskite with strong oxygen octahedron rotations. The above property is clearly represented by the large mode amplitudes of $Q_{R_{xy}}$ and $Q_{R_z^i}$, which correspond to an OOR around [110] and an in-phase OOR around [001] as shown in Table III. Under such a pattern of OORs, the antipolar mode $Q_{AFE_{xy}}$ is favored, and FE is strongly suppressed, resulting in zero polarization along all directions. On the other hand, $A''\text{BO}_3$ is a strong “cubic” perovskite [29–31] that does not display structural distortions associated with either OORs or polarization at its ground state, as shown in Table III.

Strikingly, when $A'\text{BO}_3$ and $A''\text{BO}_3$ form a $1A'\text{BO}_3/1A''\text{BO}_3$ superlattice, the resulting structural distortions are significantly different from their parent bulks. The differences come not only from the amplitudes of the modes but also from the symmetries associated with these modes. In Table III, the OORs around [110] $Q_{R_{xy}}$ are preserved in all these superlattices but with largely reduced mode amplitudes compared with those in bulk $A'\text{BO}_3$. In contrast, the in-phase OOR around [001] $Q_{R_z^i}$ completely disappears and is replaced by a large mode amplitude $Q_{R_z^o}$ associated with an out-of-phase OOR around the same axis in all the predicted new materials. As we have seen repeatedly in the previous discussions, such a new pattern of OOR signifies the stabilization of a BFO-like structure in all these artificial materials. Accordingly, large polarizations develop along both the [001] and [110] directions with the generated total polarization vector roughly along the [111] direction due to the broken symmetry in the $e-R3c$ phase. It can be noted that the polarization of BiFeO_3 is exactly along the [111] direction in the $R3c$ symmetry.

At the same time, the antipolar mode $Q_{AFE_{xy}}$ is completely eliminated. Here, we want to stress that none of the component perovskites in the predicted superlattices is polar either in its natural bulk or in its strained bulk formats.

V. OUTLOOK

Currently, there are two widely adopted interface approaches to induce FE in oxide superlattices, namely, tricolor [10] and hybrid improper methods [32]. An artificially induced broken inversion symmetry lies at the heart of both of the above methods. In the former, the broken inversion symmetry along the out-of-plane direction is introduced by the number of species in the superlattice, while in the latter, the broken inversion symmetry along the in-plane direction is facilitated by the differences in the antipolar modes of the two perovskite materials across the interface. However, it should be noted that the interface approach discussed here is a new route that is conceptually different from the above. Instead of introducing artificial inversion symmetry breaking, the ferroelectric polarization is stabilized by favoring a BFO-like structure that is a metastable phase for many perovskite materials. Because of the nature of the energy term that stabilizes the BFO-like structure (similar to $R_z^o R_{xy} FE_z FE_{xy}$), we expect that the switching of FE does not necessarily require switching the directions of oxygen octahedron rotations, which usually requires much larger energy as is implied in the hybrid improper mechanism. Indeed, the FE polarization switching has already been successfully demonstrated in 2BTO/2CTO by Lee’s group [33]. Based on nudged elastic-band (transition-state) theory [34,35] and single-domain assumption, the energy barrier in switching FE in 2BTO/2CTO (154 meV) is found to be close to that of the predicted materials $1\text{CdSnO}_3/1\text{BaSnO}_3$ (119 meV), both of which are modeled in 40-atom supercells.

In conclusion, by combining HRTEM experimental and first-principles approaches, we introduced a comprehensive interface design method to stabilize a highly polar BFO-like metastable phase in perovskite materials. Both the electric and mechanical boundary conditions are taken into account as well. This scheme introduces a conceptually novel way to design artificial FE materials. By predicting some new materials, we demonstrate this approach of exploring novel functional materials. For example, if the FE could be recovered in orthogonal RFeO₃ (R = Y, Gd, Tb, Dy, Ho, Er, Tm, Yb, Lu) [36–38] by this approach, the synthesis of a new family of room temperature multiferroic materials could be achieved. Furthermore, the result of our current work indicates that, through an interface design mechanism, short-period superlattices can have stronger FE than longer ones. This is promising for modern device applications based on ultrathin films.

ACKNOWLEDGMENTS

This research was primarily supported as part of the Center for the Computational Design of Functional Layered Materials, an Energy Frontier Research Center funded by the U.S. Department of Energy, Office of Science, Basic Energy Sciences under Award No. DE-SC0012575 (the main ideas, theoretical models, calculations, and the analysis), by National Science Foundation (NSF) under Award No. DMR-1334428 (some of the first-principles calculations), and by U.S. Department of Energy, Office of Science, Basic Energy Sciences, Materials Sciences and Engineering Division (superlattice synthesis). The transmission electron microscopy was accomplished at the Electron Microscopy Center in the Center for Nanoscale Materials at Argonne National Laboratory, a DOE-BES Facility, supported under Contract No. DE-AC02-06CH11357 by UChicago Argonne, LLC. This research used resources of the National Energy Research Scientific Computing Center (NERSC), a DOE Office of Science User Facility supported by the Office of Science of the U.S. Department of Energy under Contract No. DE-AC02-05CH11231. We thank Dr. Hua Zhou for useful discussions. X. W. is grateful for the useful discussions with Dr. Andrew J. Shanahan at University Medical Center of Princeton.

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- layer-by-layer decompositions for $2\text{BaTiO}_3/2\text{CaTiO}_3$ and $2\text{KNbO}_3/2\text{AgNbO}_3$; (9) experimental conditions and details of density functional theory calculations.
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